

# CS 352

# Network: Routing

Lecture 23

<http://www.cs.rutgers.edu/~sn624/352-F22>

Srinivas Narayana

Routing is a fundamental problem in networking.

How would one design a “Google Maps”  
to navigate the Internet?



# Per-router control plane

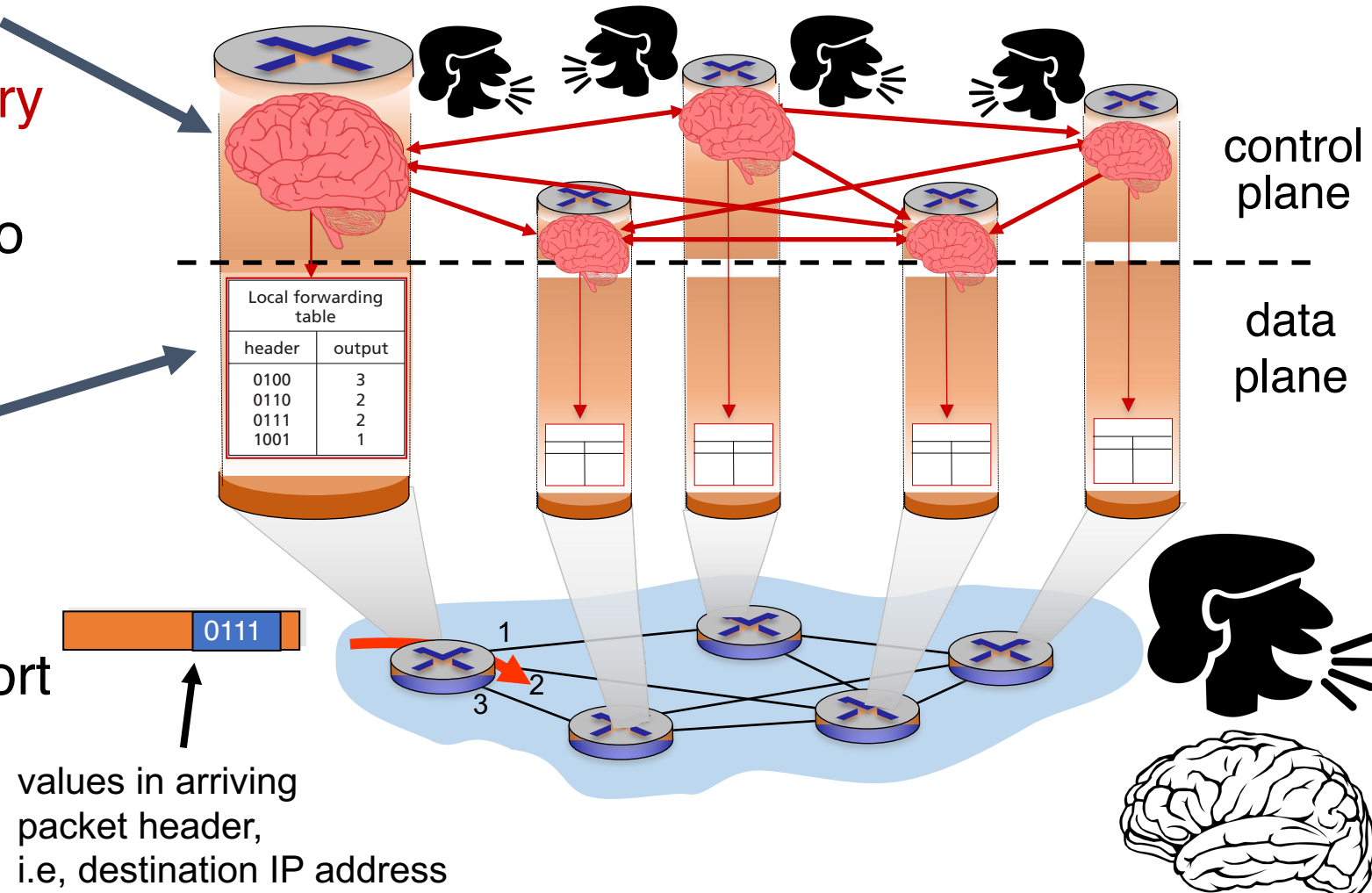
## Distributed

### control plane:

Components in **every router** interact with other components to produce a routing outcome.

### Data plane

per-packet processing, moving packet from input port to output port



## Routing protocol

Q1. What info exchanged?

Q2. What computation?

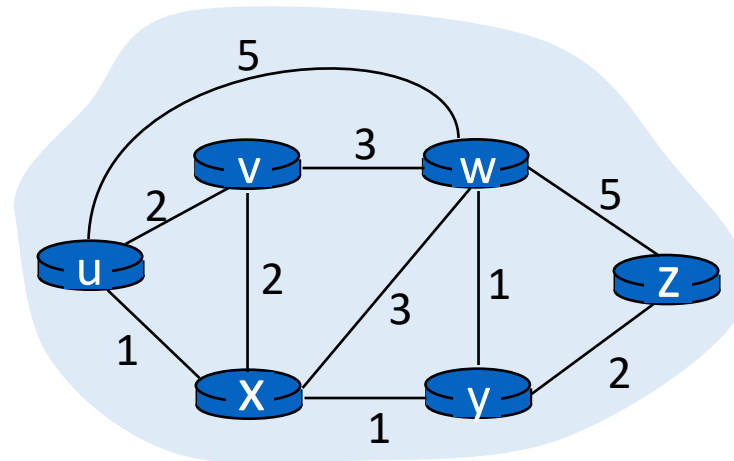
# The graph abstraction

- Routing algorithms work over an abstract representation of a network: **the graph abstraction**

Ex: Rutgers campus

u: Computer Science  
v: School of Engineering

...



- Each router is a **node** in a graph
- Each link is an **edge** in the graph
- Edges have **weights** (also called **link metrics**). Set by netadmin

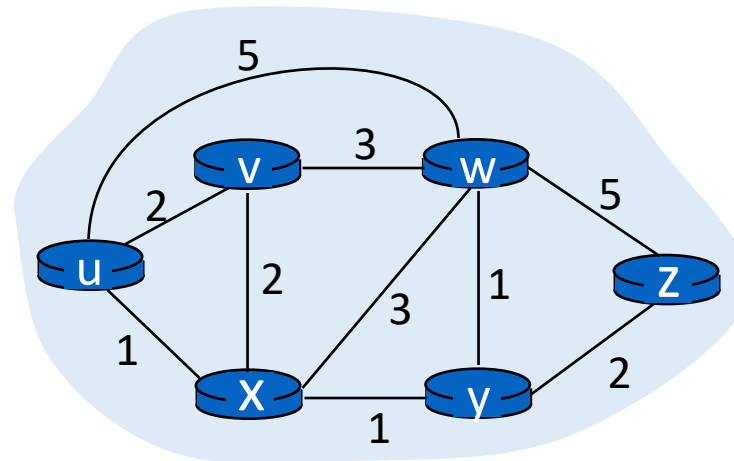
# The graph abstraction

- Routing algorithms work over an abstract representation of a network: **the graph abstraction**

Ex: Rutgers campus

u: Computer Science  
v: School of Engineering

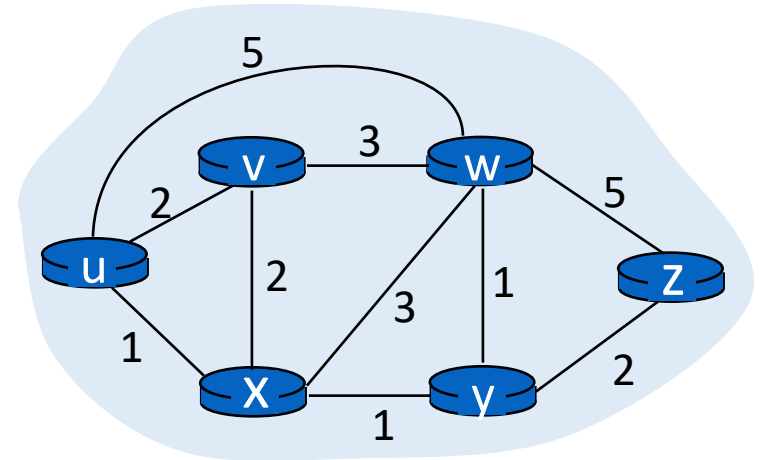
...



- $G = (N, E)$
- $N = \{u, v, w, x, y, z\}$
- $E = \{ (u,v), (u,x), (v,x), (v,w), (x,w), (x,y), (w,y), (w,z), (y,z) \}$

# The graph abstraction

- Cost of an edge:  $c(x, y)$ 
  - Examples:  $c(u, v) = 2$ ,  $c(u, w) = 5$
- Cost of a path = **sum of edge costs**
  - $c(\text{path } x \rightarrow w \rightarrow y \rightarrow z) = 3 + 1 + 2 = 6$



- **Outcome** of routing: each node should determine the **least cost path** to every other node
- Q1: What **information** should nodes **exchange** with each other to enable this computation?
- Q2: What **algorithm** should each node run to compute the least cost path to every node?

# Coming up next

## Routing protocols



### Link state protocols

Each router has **complete information** of the graph

Messages exchanged by **flooding** all over the network

Communication expensive, but complete

### Distance vector protocols

Each router only maintains **distances & next hop** to others

Messages are exchanged over each link and **stay within the link**

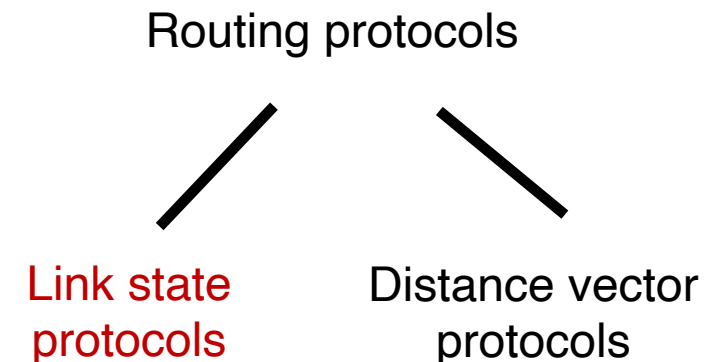
Communication cheap, but incomplete

# Link State Protocols



# Link state protocol

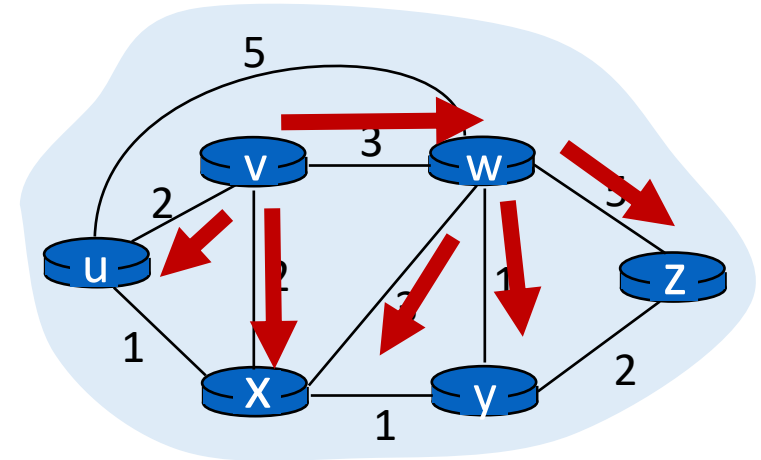
- Each router knows the **state** of all the links and routers in the network
- Every router performs an **independent** computation on **globally shared** knowledge of network's **complete** graph representation



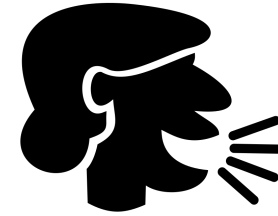
# Q1: Information exchange



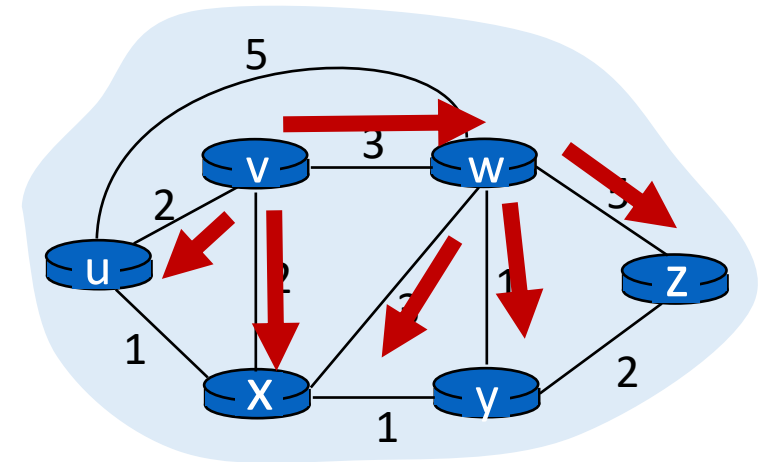
- **Link state flooding**: the process by which neighborhood information of **each network router** is transmitted to **all other routers**
- Each router sends a **link state advertisement (LSA)** to each of its neighbors
- LSA contains the router ID, the IP prefix owned by the router, the router's neighbors, and link cost to those neighbors
- Upon receiving an LSA, a router forwards it to each of its neighbors: **flooding**



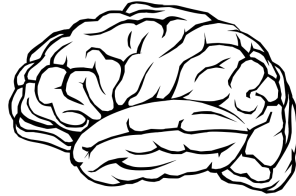
# Q1: Information exchange



- Eventually, the entire network receives LSAs originated by each router
- LSAs put into a **link state database**
- LSAs occur periodically and **whenever the graph changes**
  - Example: if a link fails
  - Example: if a new link or router is added
- The routing algorithm running at each router can **use the entire network's graph** to compute least cost paths



# Q2: The algorithm



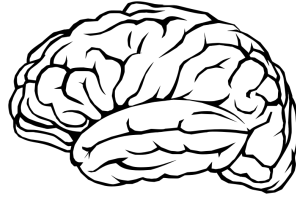
## Dijkstra's algorithm

- Given a network graph, the algorithm computes the least cost paths from one node (**source**) to all other nodes
- This can then be used to compute the **forwarding table** at that node
- Iterative algorithm: maintain **estimates** of least costs to reach every other node. After  $k$  iterations, each node definitively knows the least cost path to  $k$  destinations

## Notation:

- **$c(x,y)$** : link cost from node  $x$  to  $y$ ;  
=  $\infty$  if not direct neighbors
- **$D(v)$** : current estimate of cost of path from source to destination  $v$
- **$p(v)$** : (**predecessor node**) the last node before  $v$  on the path from source to  $v$
- **$N'$** : set of nodes whose least cost path is definitively known

# Dijkstra's Algorithm



```
1 Initialization:  
2  $N' = \{u\}$   
3 for all nodes  $v$   
4   if  $v$  adjacent to  $u$   
5     then  $D(v) = c(u,v)$   
6   else  $D(v) = \infty$   
7
```

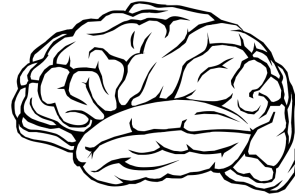
Initial estimates of distances are just the link costs of neighbors.

```
8 Loop  
9 find  $w$  not in  $N'$  such that  $D(w)$  is a minimum  
10 add  $w$  to  $N'$   
11 update  $D(v)$  for all  $v$  adjacent to  $w$  and not in  $N'$  :  
12    $D(v) = \min( D(v), D(w) + c(w,v) )$   
13   /* new cost to  $v$  is either old cost to  $v$  or known  
14   shortest path cost to  $w$  plus cost from  $w$  to  $v$  */  
15 until all nodes in  $N'$ 
```

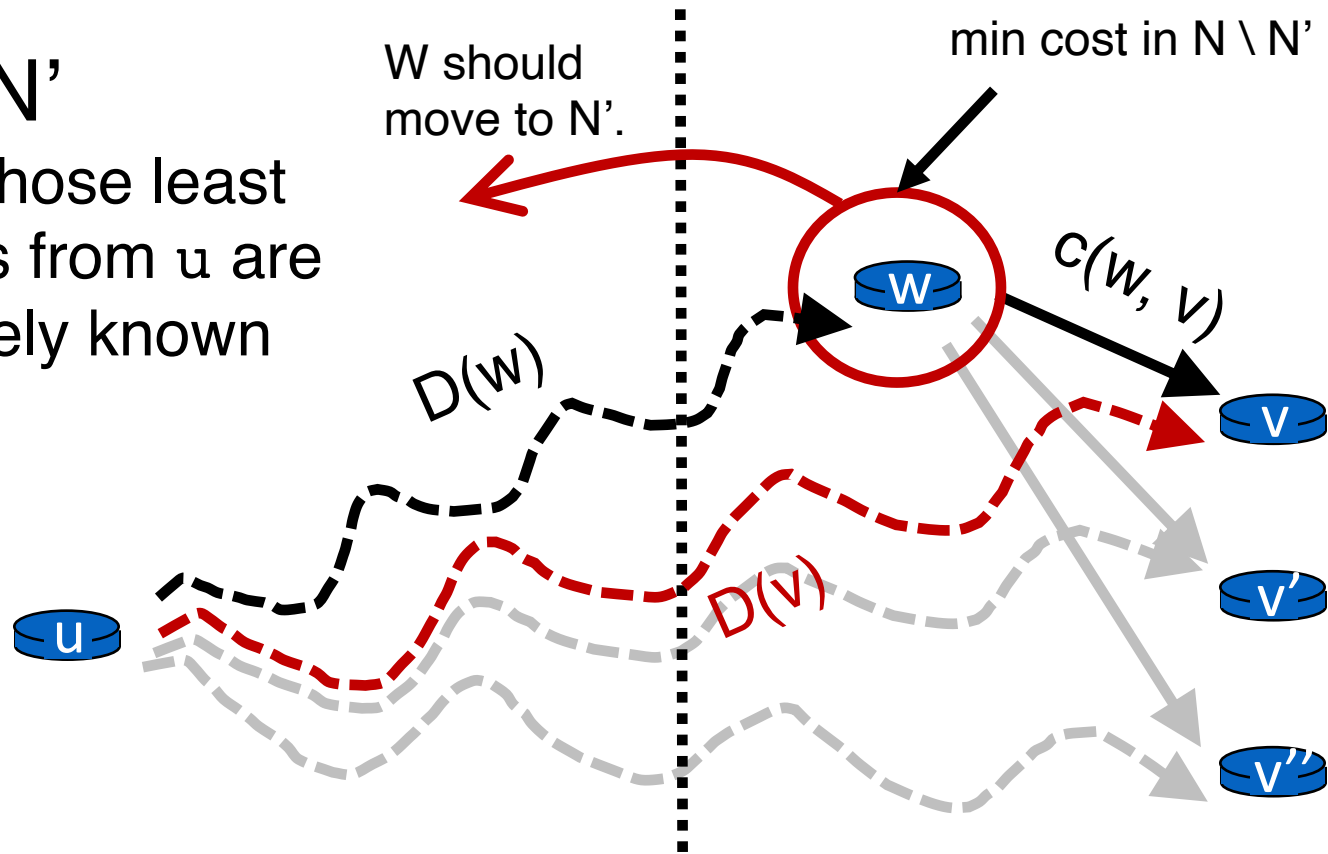
Least cost node among all estimates. This cost cannot decrease further.

**Relaxation**

# Visualization



$N'$   
nodes whose least  
cost paths from  $u$  are  
definitively known



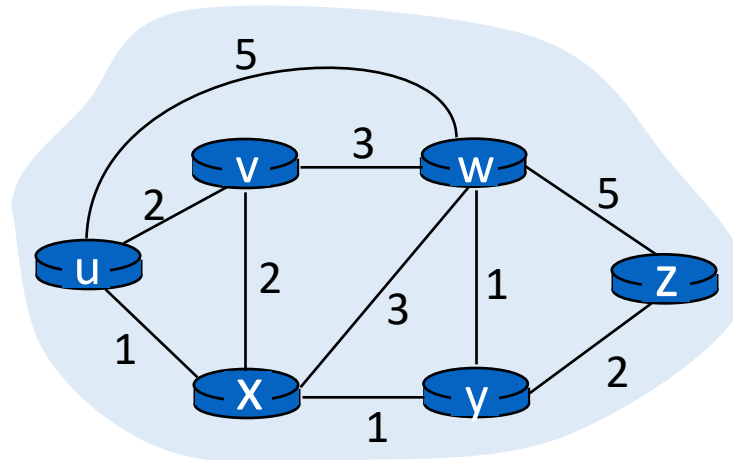
$N \setminus N'$   
Nodes with **estimated**  
least path costs, not  
definitively known to  
be smallest possible

Cost of path via  $w$ :  $D(w) + c(w, v)$   
Cost of known best path:  $D(v)$

**Relaxation**: for each  $v$   
in  $N \setminus N'$ , is the cost of  
the path via  $w$  smaller  
than known least cost  
path to  $v$ ?  
If so, **update  $D(v)$**   
**Predecessor of  $v$  is  $w$ .**

# Dijkstra's algorithm: example

Step	N'	D(v),p(v)	D(w),p(w)	D(x),p(x)	D(y),p(y)	D(z),p(z)
0	u	2,u	5,u	1,u	$\infty$	$\infty$
1	ux	2,u	4,x		2,x	$\infty$
2	uxy	2,u	3,y			4,y
3	uxyv		3,y			4,y
4	uxyvw					4,y
5	uxyvwz					



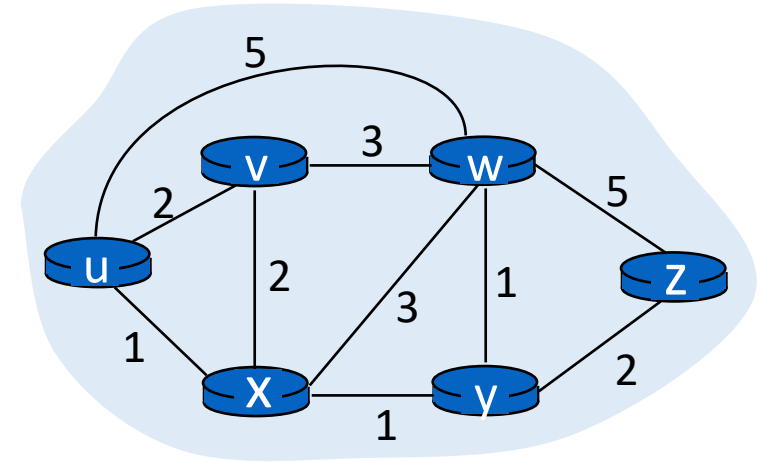
# Constructing the forwarding table

- To find the router port to use for a given destination (router), find the predecessor of the node iteratively until reaching an immediate neighbor of the source  $u$
- The port connecting  $u$  to this neighbor is the output port for this destination



# Constructing the forwarding table

- Suppose we want forwarding entry for z.



$D(v), p(v)$	$D(w), p(w)$	$D(x), p(x)$	$D(y), p(y)$	$D(z), p(z)$
2, u	3, y	1, u	2, x	4, y

$z: p(z) = y$   
 $y: p(y) = x$   
 $x: p(x) = u$   
 x is an immediate neighbor of u

Forwarding table at u:	destination	link
	z	(u, x)

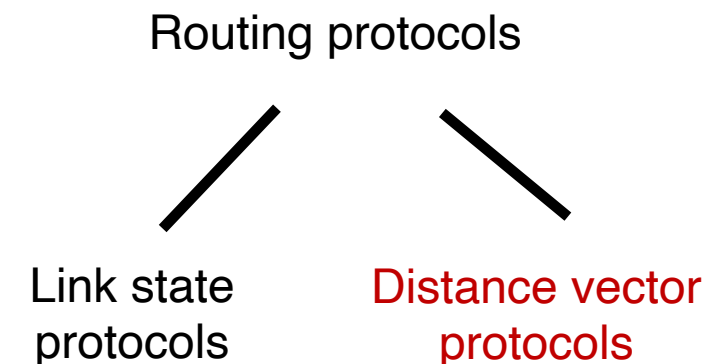
# Summary of link state protocols

- Each router announces link state to the entire network using flooding
- Each node independently computes least cost paths to every other node using the full network graph
- Dijkstra's algorithm can efficiently compute these best paths
  - Easy to populate the forwarding table from predecessor information computed during the algorithm

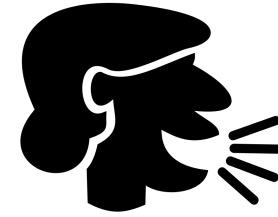
# Distance Vector Protocols

# Distance Vector Protocol

- Each router only exchanges a **distance vector** with its neighbors
  - Distance: how far the destination is
  - Vector: a value for each destination
- DVs are only exchanged between neighbors; not flooded
- Use **incomplete** view of graph **derived from neighbors'** distance vectors to compute the shortest paths

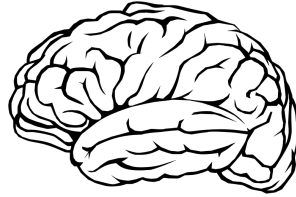


# Q1: Distance Vectors



- $D_x(y)$  = **estimate** of least cost from  $x$  to  $y$
- Distance vector:  $\mathbf{D}_x = [D_x(y): y \in N]$
- Node  $x$  knows cost of edge to each neighbor  $v$ :  $c(x,v)$
- Node  $x$  maintains  $\mathbf{D}_x$
- Node  $x$  also maintains its neighbors' distance vectors
  - For each neighbor  $v$ ,  $x$  maintains  $\mathbf{D}_v = [D_v(y): y \in N]$
- Nodes exchange distance vector periodically and **whenever the local distance vector changes** (e.g., link failure, cost changes)

# Q2: Algorithm



## Bellman-Ford algorithm

- Each node initializes its own distance vector (DV) to edge costs
- Each node sends its DVs to its neighbors
- When a node  $x$  receives new DV from a neighbor  $v$ , it updates its own DV using the **Bellman-Ford equation**:
- Given  $d_x(y) :=$  estimated cost of the least-cost path from  $x$  to  $y$
- **Update  $d_x(y) = \min_v \{c(x,v) + d_v(y)\}$**

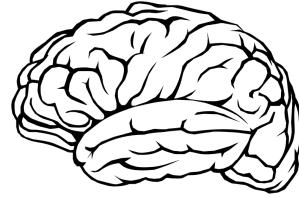
minimum taken over  
all neighbors  $v$  of  $x$

cost to reach neighbor  $v$  directly from  $x$

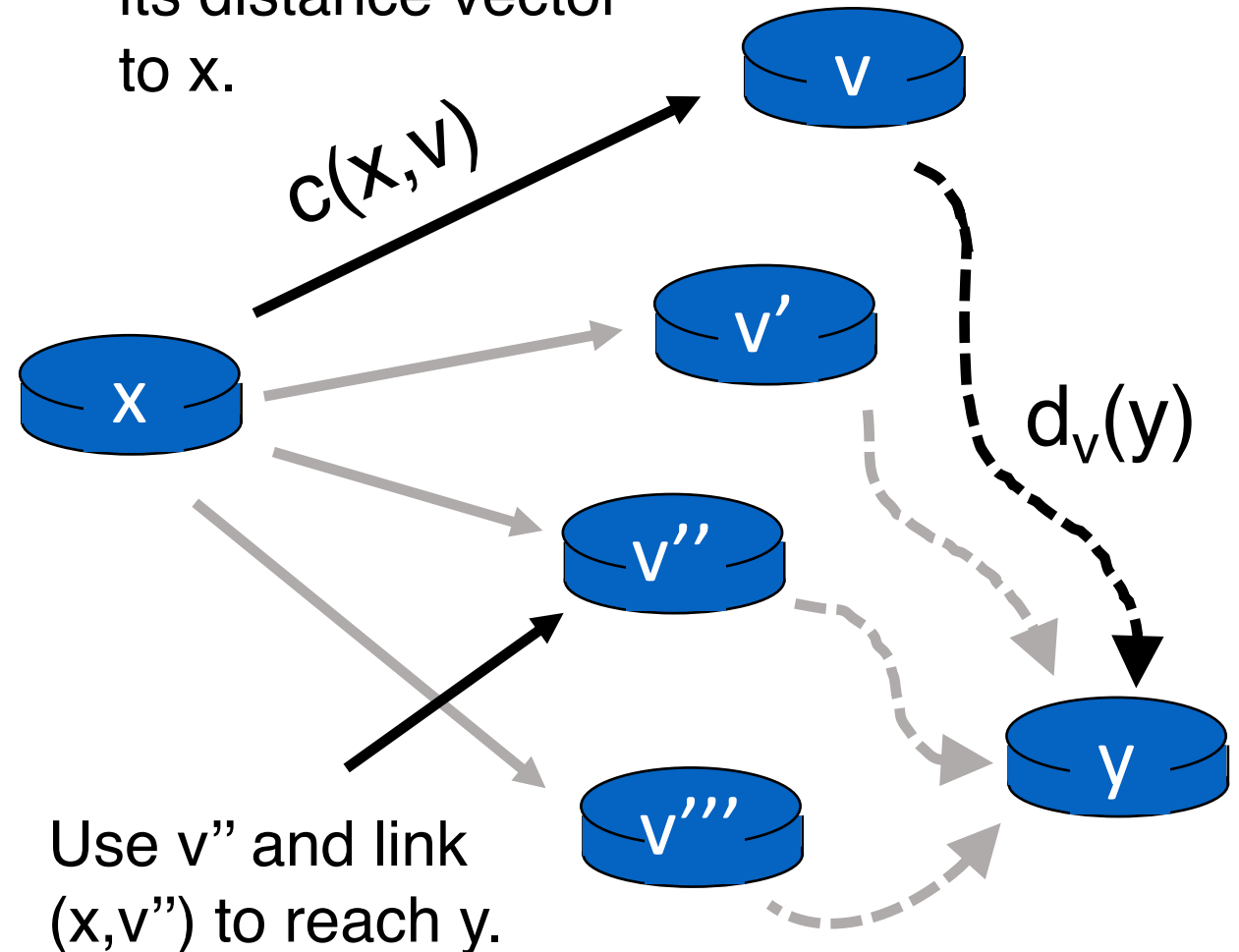
cost of path from neighbor  $v$  to destination  $y$

# Visualization

- Which neighbor  $v$  offers the current best path from  $x$  to  $y$ ?
- Path through neighbor  $v$  has cost  $c(x,v) + d_v(y)$
- Choose min-cost neighbor
- Remember **min-cost neighbor** as the one used to reach node  $y$
- This neighbor determines the output port!



Neighbor  $v$  sends its distance vector to  $x$ .



$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\}$$

$$= \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\}$$

$$= \min\{2+1, 7+0\} = 3$$

**node x table**

		cost to		
		x	y	z
from	x	0	2	7
	y	$\infty$	$\infty$	$\infty$
	z	$\infty$	$\infty$	$\infty$

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0

**node y table**

		cost to		
		x	y	z
from	x	$\infty$	$\infty$	$\infty$
	y	2	0	1
	z	$\infty$	$\infty$	$\infty$

		cost to		
		x	y	z
from	x	0	2	7
	y	2	0	1
	z	7	1	0

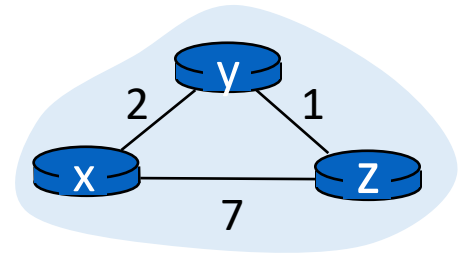
		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0

**node z table**

		cost to		
		x	y	z
from	x	$\infty$	$\infty$	$\infty$
	y	$\infty$	$\infty$	$\infty$
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	7
	y	2	0	1
	z	3	1	0

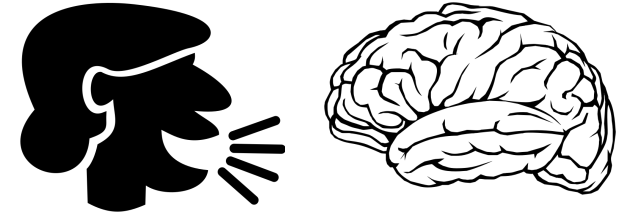
		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0



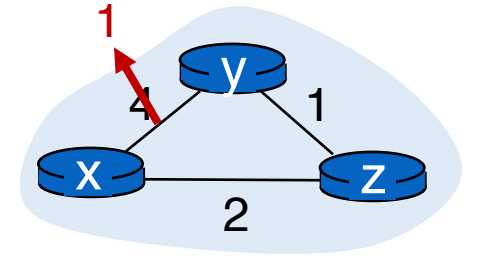
time →



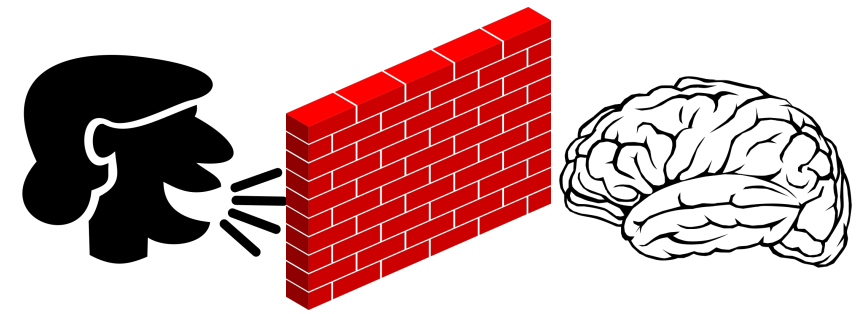
# Good news travels fast



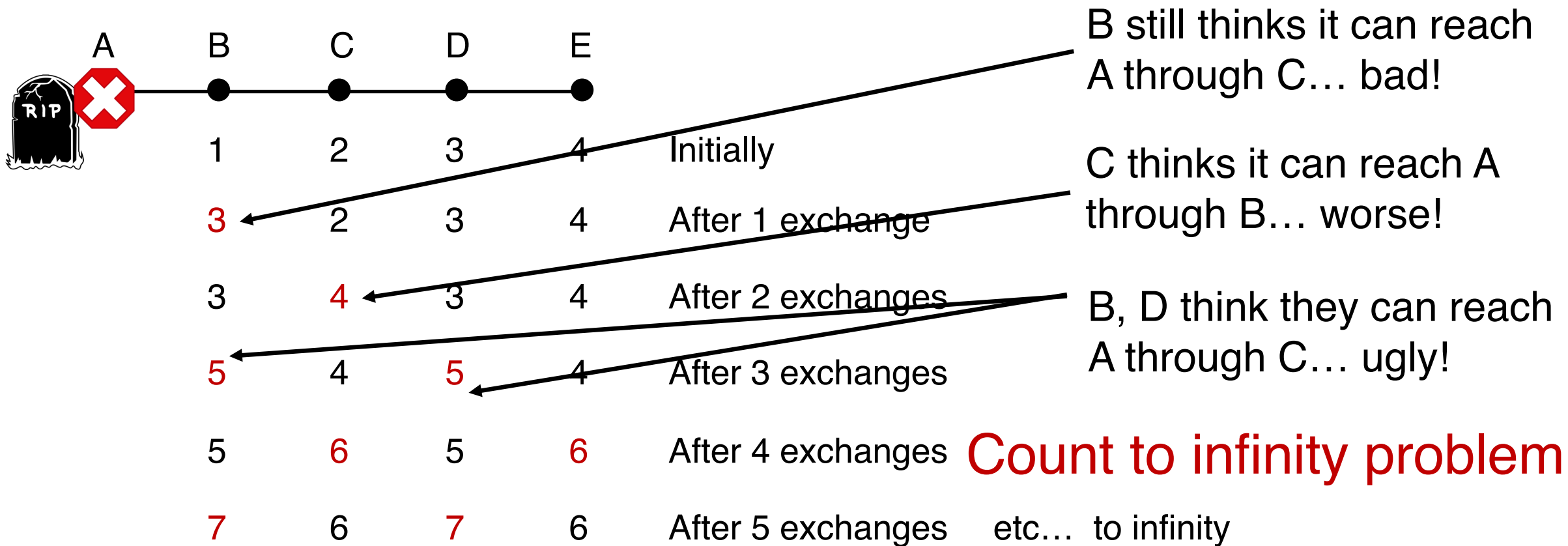
- Suppose the link cost reduces or a new better path becomes available in a network.
- The immediate neighbors of the change detect the better path immediately
- Since their DV changed, these nodes notify their neighbors immediately.
  - And those neighbors notify still more neighbors
  - ... until the entire network knows to use the better path
- **Good news travels fast** through the network
- This is **despite** messages **only being exchanged among neighbors**



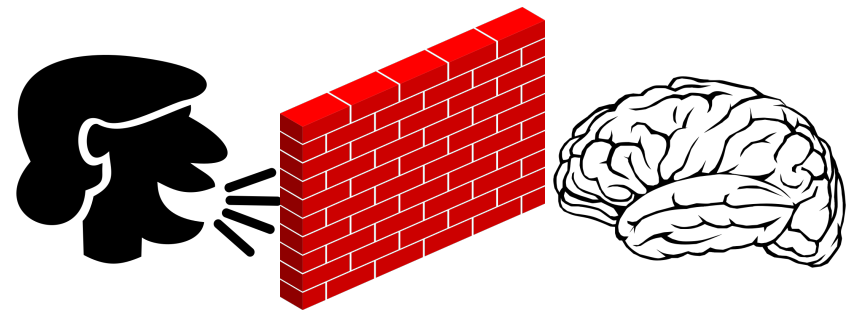
# Bad news travels slowly



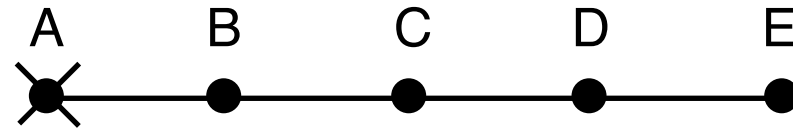
- If router goes down, could be a while before network realizes it.



# Bad news travels slowly



- Reacting appropriately to bad news requires information that only other routers have. **DV does not exchange sufficient info.**



- B needs to know that C has no other path to A other than via B.
- **DV does not exchange paths; just distances!**
- **Poisoned reverse:** if X gets its route to Y via Z, then X will announce  $d_x(Y) = \infty$  in its message to Z
  - Effect: Z won't use X to route to Y
  - However, this won't solve the problem in general (think why.)

# Summary: Comparison of LS and DV

## Link State Algorithms

- Nodes have full visibility into the network's graph
- Copious message exchange: each LSA is flooded over the whole network
- Robust to network changes and failures

### OSPF

Open Shortest Path First  
(v2 RFC 2328)

## Distance Vector Algorithms

- Only distances and neighbors are visible
- Sparse message exchange: DVs are exchanged among neighbors only
- Brittle to router failures. Incorrect info may propagate all over net

### EIGRP

Enhanced Interior Gateway Routing Protocol  
(RFC 7868)