Dynamic Backdoor Attacks Against Machine Learning Models

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Abstract—Machine learning (ML) has made tremendous progress during the past decade and is being adopted in various critical real-world applications. However, recent research has shown that ML models are vulnerable to multiple security and privacy attacks. In particular, backdoor attacks against ML models have recently raised a lot of awareness. A successful backdoor attack can cause severe consequences, such as allowing an adversary to bypass critical authentication systems.

Current backdooring techniques rely on adding static triggers (with fixed patterns and locations) on ML model inputs. In this paper, we propose the first class of dynamic backdooring techniques: Random Backdoor, Backdoor Generating Network (BaN), and conditional Backdoor Generating Network (c-BaN). Triggers generated by our techniques can have random patterns and locations, which reduce the efficacy of the current backdoor detection mechanisms. In particular, BaN and c-BaN are the first two schemes that algorithmically generate triggers, which rely on a novel generative network. Moreover, c-BaN is the first conditional backdooring technique, that given a target label, it can generate a target-specific trigger. Both BaN and c-BaN are essentially a general framework which renders the adversary the flexibility for further customizing backdoor attacks.

We extensively evaluate our techniques on three benchmark datasets: MNIST, CelebA, and CIFAR-10. Our techniques achieve almost perfect attack performance on backdoored data with a negligible utility loss. We further show that our techniques can bypass current state-of-the-art defense mechanisms against backdoor attacks, including Neural Cleanse, ABS, and STRIP.

I. INTRODUCTION

Machine learning (ML), represented by Deep Neural Network (DNN), has made tremendous progress during the past decade, and ML models have been adopted in a wide range of real-world applications including those that play critical roles. For instance, Apple’s FaceID [1] is using ML-based facial recognition systems for unlocking the mobile device and authenticating purchases in Apple Pay. However, recent research has shown that machine learning models are vulnerable to various security and privacy attacks, such as evasion attacks [33], [32], [48], membership inference attacks [39], [37], model stealing attacks [44], [29], [46], data poisoning attacks [5], [17], [42], Trojan attacks [22], and backdoor attacks [49], [12].

In this work, we focus on backdoor attacks against DNN models on image classification tasks, which are among the most successful ML applications deployed in the real world. In the backdoor attack setting, an adversary trains an ML model which can intentionally misclassify any input with an added trigger (a secret pattern constructed from a set of neighboring pixels, e.g., a white square) to a specific target label. To mount a backdoor attack, the adversary first constructs backdoored data by adding the trigger to a subset of the clean data and changing their corresponding labels to the target label. Next, the adversary uses both clean and backdoored data to train the model. The clean and backdoored data are needed so the model can learn its original task and the backdoor behavior, simultaneously. Backdoor attacks can cause severe security and privacy consequences. For instance, an adversary can implant a backdoor in an authentication system to grant herself unauthorized access.

Current state-of-the-art backdoor attacks [12], [22], [49] generate static triggers, in terms of fixed trigger pattern and location (on the input). For instance, Figure 1a shows an example of triggers constructed by Badnets [12], one of the most popular backdoor attack methods. As we can see, Badnets in this case uses a white square as a trigger and always places it in the top-left corner of all inputs. Recent proposed defense mechanisms [47], [21] leverage the static property of triggers to detect whether an ML model is backdoored or not.

A. Our Contributions

In this work, we propose the first class of backdooring techniques against ML models that generate dynamic triggers, in terms of trigger pattern and location. We refer to our techniques as dynamic backdoor attacks. Dynamic backdoor attacks offer the adversary more flexibility, as they allow triggers to have different patterns and locations. Moreover, our techniques largely reduce the efficacy of the current defense mechanisms demonstrated by our empirical evaluation. Figure 1b shows an example of our dynamic backdoor attacks implemented in a model trained on the CelebA dataset [23]. In addition, we extend our techniques to work for all labels of the backdoored ML model, while the current backdoor attacks only focus on a single or a few target labels. This further increases the difficulty of our backdoors being mitigated.

In total, we propose 3 different dynamic backdoor techniques, namely, Random Backdoor, Backdoor Generating Network (BaN), and conditional Backdoor Generating Network (c-BaN). In particular, the latter two attacks algorithmically generate triggers to mount backdoor attacks which are first of their kind. In the following, we abstractly introduce each of our techniques.
Random Backdoor: In this approach, we construct triggers by sampling them from a uniform distribution. Then, we place each randomly generated trigger at a random location for each input, which is then mixed with clean data to train the backdoor model.

Backdoor Generating Network (BaN): In our second technique, we propose a generative ML model, i.e., BaN, to generate triggers. To the best of our knowledge, this is the first backdoor attack which uses a generative network to automatically construct triggers, which increases the flexibility of the adversary to perform backdoor attacks. BaN is trained jointly with the backdoor model, it takes a latent code sampled from a uniform distribution to generate a trigger, then place it at a random location on the input, thus making the trigger dynamic in terms of pattern and location. Moreover, BaN is essentially a general framework under which the adversary can change and adapt its loss function to her requirements. For instance, if there is a specific backdoor defense in place, the adversary can evade the defense by adding a tailored discriminative loss in BaN.

conditional Backdoor Generating Network (c-BaN): Both of our Random Backdoor and the BaN techniques can implement a dynamic backdoor for either a single target label or multiple target labels. However, for the case of the multiple target labels, both techniques require each target label to have its unique trigger locations. In other words, a single location cannot have triggers for different target labels.

Our last and most advanced technique overcomes the previous two techniques’ limitation of having disjoint location sets for the multiple target labels. In this technique, we transform the BaN into a conditional BaN (c-BaN), to force it to generate label specific triggers. More specifically, we modify the BaN’s architecture to include the target label as the input, to generate a trigger for this specific label. This target specific triggers property, allows the triggers for different target labels to be positioned at any location. In other words, each target label does not need to have its unique trigger locations.

To demonstrate the effectiveness of our proposed techniques, we perform empirical analysis with three ML model architectures over three benchmark datasets. All of our techniques achieve almost a perfect backdoor accuracy, i.e., the accuracy of the backdoored model on the backdoored data is approximately 100%, with a negligible utility loss. For instance, our BaN trained models on CelebA [23] and MNIST [2] datasets achieve 70% and 99% accuracy, respectively, which is the same accuracy as the clean model. Also, c-BaN, BaN, and Random Backdoor trained models achieve 92%, 92.1%, and 92% accuracy on the CIFAR-10 [3] dataset, respectively, which is almost the same as the performance of a clean model (92.4%). Moreover, we evaluate our techniques against three of the current state-of-the-art backdoor defense techniques, namely Neural Cleanse [47], ABS [21], and STRIP [10]. Our results show that our techniques can bypass these defenses.

In general, our contributions can be summarized as the following:

- We broaden the class of backdoor attacks by introducing the dynamic backdoor attacks.
- We propose both Backdoor Generating Network (BaN) and conditional Backdoor Generating Network (c-BaN), which are the first algorithmic backdoor paradigm.
- Our dynamic backdoor attacks achieve strong performance, while bypassing the current state-of-the-art backdoor defense techniques.

B. Organization

We first present the necessary background knowledge in Section II, then we introduce our different dynamic backdoor techniques in Section III. Section IV evaluates the performance of our different techniques and the effect of their hyperparameters. Finally, we present the related works in Section V and conclude the paper in Section VI.
II. PRELIMINARIES

In this section, we first introduce the machine learning classification setting. Then we formalize backdoor attacks against ML models, and finally, we discuss the threat model we consider throughout the paper.

A. Machine Learning Classification

A machine learning classification model \( \mathcal{M} \) is essentially a function that maps a feature vector \( x \) from the feature space \( \mathcal{X} \) to an output vector \( y \) from the output space \( \mathcal{Y} \), i.e.,

\[
\mathcal{M}(x) = y.
\]

Each entry \( y_i \) in the vector \( y \) corresponds to the posterior probability of the input vector \( x \) being affiliated with the label \( \ell_i \in \mathcal{L} \), where \( \mathcal{L} \) is the set of all possible labels. In this work, instead of \( y \), we only consider the output of \( \mathcal{M} \) as the label with the highest probability, i.e.,

\[
\mathcal{M}(x) = \arg\max_{\ell_i} y
\]

To train \( \mathcal{M} \), we need a dataset \( \mathcal{D} \) which consists of pairs of labels and features vectors, i.e., \( \mathcal{D} = \{(x_i, \ell_i)\}_{i \in \mathcal{X}} \) with \( \mathcal{N} \) being the size of the dataset, and adopt some optimization algorithm, such as Adam, to learn the parameters of \( \mathcal{M} \) following a defined loss function.

B. Backdoor in Machine Learning Models

Backdooring is the general technique of hiding a -usually-malicious functionality in the system, that can be only triggered with a certain secret/backdoor. For instance, an adversary can implement a backdoor into an authentication system to access any desired account. An example trigger in this use case can be a secret password that works with all possible accounts. An important requirement of backdoors is that the system should behave normally on all inputs except the ones with triggers.

Intuitively, a backdoor in the ML settings resembles a hidden behavior of the model, which only happens when it is queried with an input containing a secret trigger. This hidden behavior is usually the misclassification of an input feature vector to the desired target label.

A backdoored model \( \mathcal{M}_{bd} \) is expected to learn the mapping from the feature vectors with triggers to their corresponding target label, i.e., any input with the trigger \( t_i \) should have the label \( \ell_i \) as its output. To train such a model, an adversary needs both clean data \( \mathcal{D}_c \) (to preserve the model’s utility) and backdoored data \( \mathcal{D}_{bd} \) (to implement the backdoor behaviour), where \( \mathcal{D}_{bd} \) is constructed by adding triggers to a subset of \( \mathcal{D}_c \).

Current backdoor attacks construct backdoors with static triggers, in terms of fixed trigger pattern and location (on the input). In this work, we introduce dynamic backdoors, where the trigger pattern and location are dynamic. In other words, a dynamic backdoor should have triggers with different values (pattern) and can be placed at different positions on the input (location).

More formally, a backdoor in an ML model is associated with a set of triggers \( \mathcal{T} \), set of target labels \( \mathcal{L}' \), and a backdoor adding function \( \mathcal{A} \). We first define the backdoor adding function \( \mathcal{A} \) as follows:

\[
\mathcal{A}(x, t_i, \kappa) = x_{bd}
\]

where \( x \) is the input vector, \( t_i \in \mathcal{T} \) is the trigger, \( \kappa \) is the desired location to add the backdoor -more practically the location of the top left corner pixel of the trigger-, and \( x_{bd} \) is the input vector \( x \) with the backdoor inserted at the location \( \kappa \).

Compared to the static backdoor attacks, dynamic backdoor attacks introduce new features for the triggers, which give the adversary more flexibility and increase the difficulty of detecting such backdoors. Namely, dynamic backdoors introduce different locations and patterns for the backdoor triggers. These multiple patterns and locations for the triggers harden the detection of such backdoors, since the current design of defenses assumes a static behavior of backdoors. Moreover, these triggers can be algorithmically generated ones, as will be shown later in Section III-B and Section III-C, which allows the adversary to customize the generated triggers.

C. Threat Model

As previously mentioned, backdooring is a training time attack, i.e., the adversary is the one who trains the ML model. To achieve this, we assume the adversary can access the data used for training the model, and control the training process. Then, the adversary publishes the backdoored model to the victim. To launch the attack, the adversary first adds a trigger to the input and then uses it to query the backdoored model. This added trigger makes the model misclassify the input to the target label. In practice, this can allow an adversary to bypass authentication systems to achieve her goal. This threat model follows the same one used by previous works, such as [12].

III. DYNAMIC BACKDOORS

In this section, we propose three different techniques for performing the dynamic backdoor attack, namely, Random Backdoor, Backdoor Generating Network (BaN), and conditional Backdoor Generating Network (c-BaN).

A. Random Backdoor

We start with our simplest approach, i.e., the Random Backdoor technique. Abstractly, the Random Backdoor technique constructs triggers by sampling them from a uniform distribution, and adding them to the inputs at random locations. We first introduce how to use our Random Backdoor technique to implement a dynamic backdoor for a single target label, then we generalize it to consider multiple target labels.

Single Target Label: We start with the simple case of considering dynamic backdoors for a single target label. Intuitively, we construct the set of triggers \( \mathcal{T} \) and the set of possible locations \( \mathcal{K} \), such that for any trigger sampled from \( \mathcal{T} \) and
added to any input at a random location sampled from \( K \), the model will output the specified target label. More formally, for any location \( \kappa_i \in K \), any trigger \( t_i \in T \), and any input \( x_i \in X \):

\[
M_{bd}(A(x_i, t_i, \kappa_i)) = \ell
\]

where \( \ell \) is the target label, \( T \) is the set of triggers, and \( K \) is the set of locations.

To implement such a backdoor in a model, an adversary needs first to select her desired trigger locations, and create the set of possible locations \( K \). Then, she uses both clean and backdoored data to update the model for each epoch. More concretely, the adversary trains the model as mentioned in Section II-B with the following two differences.

- First, instead of using a fixed trigger for all inputs, each time the adversary wants to add a trigger to an input, she samples a new trigger from a uniform distribution, i.e., \( t \sim U(0, 1) \). Here, the set of possible triggers \( T \) contains the full range of all possible values for the triggers, since the trigger is randomly sampled from a uniform distribution.

- Second, instead of placing the trigger in a fixed location, she places it at a random location \( \kappa \), sampled from the predefined set of locations, i.e., \( \kappa \in K \).

Finally, this technique is not only limited to uniform distribution, but the adversary can use different distributions like the Gaussian distribution to construct the triggers.

**Multiple Target Labels:** Next, we consider the more complex case of having multiple target labels. Without loss of generality, we consider implementing a backdoor for each label in the dataset since this is the most challenging setting. However, our techniques can be applied for any smaller subset of labels. This means that for any label \( \ell_i \in \mathcal{L} \), there exists a trigger \( t \) which when added to the input \( x \) at a location \( \kappa \), will make the model \( M_{bd} \) output \( \ell_i \). More formally,

\[
\forall \ell_i \in \mathcal{L} \exists \ell, \kappa : M_{bd}(A(x, t, \kappa)) = \ell_i
\]

To achieve the dynamic backdoor behaviour in this setting, each target label should have a set of possible triggers and a set of possible locations. More formally,

\[
\forall \ell_i \in \mathcal{L} \exists \mathcal{T}_i, \mathcal{K}_i
\]

where \( \mathcal{T}_i \) is the set of possible triggers and \( \mathcal{K}_i \) is the set of possible locations for the target label \( \ell_i \).

We generalize the Random Backdoor technique by dividing the set of possible locations \( K \) into disjoint subsets for each target label, while keeping the trigger construction method the same as in the single target label case, i.e., the triggers are still sampled from a uniform distribution. For instance, for the target label \( \ell_i \), we sample a set of possible locations \( \mathcal{K}_i \), where \( \mathcal{K}_i \) is subset of \( K \) (\( \mathcal{K}_i \subset K \)). The adversary can construct the disjoint sets of possible locations as follows:

1) First, the adversary selects all possible triggers locations and constructs the set \( \mathcal{K}_i \).

2) Second, for each target label \( \ell_i \), she constructs the set of possible locations for this label \( \mathcal{K}_i \) by sampling the set \( \mathcal{K} \). Then, she removes the sampled locations from the set \( \mathcal{K} \).

We propose the following simple algorithm to assign the locations for the different target labels. However, an adversary can construct the location sets arbitrarily with the only restriction that no location can be used for more than one target label.

We uniformly split the image into non-intersecting regions, and assign a region for each target label, in which the triggers’ locations can move vertically. Figure 2 shows an example of our location setting technique for a use case with 6 target labels.

**Backdoor Generating Network (BaN)**

Next, we introduce our second technique to implement dynamic backdoors, namely, the Backdoor Generating Network (BaN). BaN is the first approach to algorithmically generate backdoor triggers, instead of using fixed triggers or sampling triggers from a uniform distribution (as in Section III-A).

BaN is inspired by the state-of-the-art generative model – Generative Adversarial Networks (GANs) [11]. However, it is different from the original GANs in the following aspects. First, instead of generating images, our BaN generator generates backdoor triggers. Second, we jointly train the BaN
generator with the target model instead of the discriminator, to learn the (generator) and implement the (target model) the best patterns for the backdoor triggers.

After training, the BaN can generate a trigger ($t_i$) for each noise vector ($z \sim U(0,1)$). This trigger is then added to an input using the backdoor adding function $A$, to create the backdoored input as shown in Figure 3a. Similar to the previous approach (Random Backdoor), the generated triggers are placed at random locations.

In this section, we first introduce the BaN technique for a single target label, then we generalize it for multiple target labels.

**Single Target Label:** We start with presenting how to implement a dynamic backdoor for a single target label, using our BaN technique. First, the adversary creates the set $K$ of the possible locations. She then jointly trains the BaN with the backdoored $M_{bd}$ model as follows:

1) The adversary starts each training epoch by querying the clean data to the backdoored model $M_{bd}$. Then, she calculates the clean loss $\varphi_c$ between the ground truth and the output labels. We use the cross-entropy loss for our clean loss, which is defined as follows:

$$\sum_{i} y_i \log(\hat{y}_i)$$

where $y_i$ is the true probability of label $\ell_i$ and $\hat{y}_i$ is our predicted probability of label $\ell_i$.

2) She then generates $n$ noise vectors, where $n$ is the batch size.

3) On the input of the $n$ noise vectors, the BaN generates $n$ triggers.

4) The adversary then creates the backdoored data by adding the generated triggers to the clean data using the backdoor adding function $A$.

5) She then queries the backdoored data to the backdoored model $M_{bd}$ and calculates the backdoor loss $\varphi_{bd}$ on the model’s output and the target label. Similar to the clean loss, we use the cross-entropy loss as our loss function for $\varphi_{bd}$.

6) Finally, the adversary updates the backdoor model $M_{bd}$ using both the clean and backdoor losses ($\varphi_c + \varphi_{bd}$) and updates the BaN with the backdoor loss ($\varphi_{bd}$).

One of the main advantages of the BaN technique is its flexibility. Meaning that it allows the adversary to customize her triggers by plugging any customized loss to it. In other words, BaN is a framework for a more generalized class of backdoors that allows the adversary to customize the desired trigger by adapting the loss function.

**Multiple Target Labels:** We now consider the more complex case of building a dynamic backdoor for multiple target labels using our BaN technique. To recap, our BaN generates general triggers and not label specific triggers. In other words, the same trigger pattern can be used to trigger multiple target labels. Thus similar to the Random Backdoor, we depend on the location of the triggers to determine the output label.

We follow the same approach of the Random Backdoor technique to assign different locations for different target labels (Section III-A), to generalize the BaN technique. More concretely, the adversary implements the dynamic backdoor for multiple target labels using the BaN technique as follows:

1) The adversary starts by creating disjoint sets of locations for all target labels.

2) Next she follows the same steps as in training the backdoor for a single target label, while repeating from step 2 to 5 for each target label and adding all their backdoor losses together. More formally, for the multiple target label case the backdoor loss is defined as:

$$\sum_{i} |L'| \varphi_{bd_i}$$

where $L'$ is the set of target labels, and $\varphi_{bd_i}$ is the backdoor loss for target label $\ell_i$.

**C. conditional Backdoor Generating Network (c-BaN)**

So far, we have proposed two techniques to implement dynamic backdoors for both single and multiple target labels, i.e,
Random Backdoor (Section III-A) and BaN (Section III-B). To recap, both techniques have the limitation of not having label specific triggers and only depending on the trigger location to determine the target label. We now introduce our third and most advanced technique, the conditional Backdoor Generating Network (c-BaN), which overcomes this limitation. More concretely, with the c-BaN technique any location $\kappa$ inside the location set $\mathcal{K}$ can be used to trigger any target label. To achieve this location independency, the triggers need to be label specific. Therefore, we convert the Backdoor Generating Network (BaN) into a conditional Backdoor Generating Network (c-BaN). More specifically, we add the target label as an additional input to the BaN for conditioning it to generate target specific triggers.

We construct the c-BaN by adding an additional input layer to the BaN, to include the target label as an input. Figure 4 represents an illustration for the structure of c-BaN. As the figure shows, the two input layers take the noise vector and the target label and encode them to latent vectors with the same size (to give equal weights for both inputs). These two latent vectors are then concatenated and used as an input to the next layer. It is important to mention that we use one-hot encoding to encode the target label before applying it to the c-BaN.

The c-BaN is trained similarly to the BaN, with the following two exceptions.

1) First, the adversary does not have to create disjoint sets of locations for all target labels (step 1), she can use the complete location set $\mathcal{K}$ for all target labels.

2) Second, instead of using only the noise vectors as an input to the BaN, the adversary one-hot encodes the target label, then use it together with the noise vectors as the input to the c-BaN.

To use the c-BaN, the adversary first samples a noise vector and one-hot encodes the label. Then she inputs both of them to the c-BaN, which generates a trigger. The adversary uses the backdoor adding function $\mathcal{A}$ to add the trigger to the target input. Finally, she queries the backdoored input to the backdoored model, which will output the target label. We visualize the complete pipeline of using the c-BaN technique in Figure 3b.

In this section, we have introduced three techniques for implementing dynamic backdoors, namely, the Random Backdoor, the Backdoor Generating Network (BaN), and the conditional Backdoor Generating Network (c-BaN). These three dynamic backdoor techniques present a framework to generate dynamic backdoors for different settings. For instance, our framework can generate target specific triggers’ pattern using the c-BaN, or target specific triggers’ location like the Random Backdoor and BaN. More interestingly, our framework allows the adversary to customize her backdoor by adapting the backdoor loss functions. For instance, the adversary can adapt to different defenses against the backdoor attack that can be modeled as a machine learning model. This can be achieved by adding any defense as a discriminator into the training of the BaN or c-BaN. Adding this discriminator will penalize/guide the backdoored model to bypass the modeled defense.

IV. Evaluation

In this section, we first introduce our datasets and experimental settings. Next, we evaluate all of our three techniques, i.e., Random Backdoor, Backdoor Generating Network (BaN), and conditional Backdoor Generating Network (c-BaN). We then evaluate our three dynamic backdoor techniques against the current state-of-the-art techniques. Finally, we study the effect of different hyperparameters on our techniques.

A. Datasets Description

We utilize three image datasets to evaluate our techniques, including MNIST, CelebA, and CIFAR-10. These three datasets are widely used as benchmark datasets for various security/privacy and computer vision tasks. We briefly describe each of them below.

**MNIST:** The MNIST dataset [2] is a 10-class dataset consisting of 70,000 grey-scale $28 \times 28$ images. Each of these images contains a handwritten digit in its center. The MNIST dataset is a balanced dataset, i.e., each class is represented with 7,000 images.

**CIFAR-10:** The CIFAR-10 dataset [3] is composed of 60,000 $32 \times 32$ colored images which are equally distributed on the following 10 classes: Airplane, automobile, bird, cat, deer, dog, frog, horse, ship, and truck.
CelebA: The CelebA dataset [23] is a large-scale face attributes dataset with more than 200K colored celebrity images, each annotated with 40 binary attributes. We select the top three most balanced attributes including Heavy Makeup, Mouth Slightly Open, and Smiling. Then we concatenate them into 8 classes to create a multiple label classification task. For our experiments, we scale the images to $64 \times 64$ and randomly sample 10,000 images for training, and another 10,000 for testing. Finally, it is important to mention that unlike the MNIST and CIFAR-10 datasets, this dataset is highly imbalanced.

B. Experimental Setup

First, we introduce the different models’ architecture for our target models, BaN, and c-BaN. Then, we introduce our evaluation metrics.

Models Architecture: For the target models’ architecture, we use the VGG-19 [40] for the CIFAR-10 dataset, and build our own convolution neural networks (CNN) for the CelebA and MNIST datasets. More concretely, we use 3 convolution layers and 5 fully connected layers for the CelebA CNN. And 2 convolution layers and 2 fully connected layers for the MNIST CNN. Moreover, we use dropout for both the CelebA and MNIST models to avoid overfitting.

For BaN, we use the following architecture:

\[
\text{Backdoor Generating Network (BaN)’s architecture:} \quad z \rightarrow \text{FullyConnected}(64) \rightarrow \text{FullyConnected}(128) \rightarrow \text{FullyConnected}(|t|) \rightarrow \text{Sigmoid} \rightarrow t
\]

Here, $\text{FullyConnected}(x)$ denotes a fully connected layer with $x$ hidden units, $|t|$ denotes the size of the required trigger, and $\text{Sigmoid}$ is the Sigmoid function. We adopt ReLU as the activation function for all layers, and apply dropout after all layers except the first and last ones.

For c-BaN, we use the following architecture:

\[
\text{conditional Backdoor Generating Network (c-BaN)’s architecture:} \quad z, \ell \rightarrow 2 \times \text{FullyConnected}(64) \rightarrow 2 \times \text{FullyConnected}(128) \rightarrow 2 \times \text{FullyConnected}(128) \rightarrow 2 \times \text{FullyConnected}(|t|) \rightarrow \text{Sigmoid} \rightarrow t
\]

The first layer consists of two separate fully connected layers, where each one of them takes an independent input, i.e., the first takes the noise vector $z$ and the second takes the target label $\ell$. The outputs of these two layers are then concatenated and used as an input to the next layer (see Section III-C).

Evaluation Metrics: We define the following two metrics to evaluate the performance of our backdoored models. The first one is the backdoor success rate, which is measured by calculating the backdoored model’s accuracy on backdoored data. The second one is model utility, which is used to measure the original functionality of the backdoored model. We quantify the model utility by comparing the accuracy of the backdoored model with the accuracy of a clean model on clean data. Closer accuracies implies a better model utility.

C. Random Backdoor

We now evaluate the performance of our first dynamic backdooring technique, namely, the Random Backdoor. We use all three datasets for the evaluation. First, we evaluate the single target label case, where we only implement a backdoor for a single target label, in the backdoored model $\mathcal{M}_{bd}$. Then we evaluate the more generalized case, i.e., the multiple target labels case, where we implement a backdoor for all possible labels in the dataset.

For both the single and multiple target label cases, we split each dataset into training and testing datasets. The training dataset is used to train the MNIST and CelebA models from scratch. For CIFAR-10, we use a pre-trained VGG-19 model. We refer to the testing dataset as the clean testing dataset, and we first use it to construct a backdoored testing dataset by adding triggers to all of its images. To recap, for the Random Backdoor technique, we construct the triggers by sampling them from uniform distribution, and add them to the images using the backdoor adding function $\mathcal{A}$. We use the backdoored testing dataset to calculate the backdoor success rate, and the training dataset to train a clean model -for each dataset- to evaluate the backdoored model’s ($\mathcal{M}_{bd}$) utility.
Fig. 6: The result of our Random Backdoor (Figure 6a), BaN (Figure 6b), and BaN with higher randomness (Figure 6c) techniques for a single target label (0).

We follow Section III-A to train our backdoored model $M_{bd}$ for both the single and multiple target labels cases. Abstractly, for each epoch, we update the backdoored model $M_{bd}$ using both the clean and backdoor losses $\varphi_c + \varphi_{bd}$. For the set of possible locations $K$, we use four possible locations.

The backdoor success rate is always 100% for both the single and multiple target labels cases on all three datasets, hence, we only focus on the backdoored model’s ($M_{bd}$) utility.

**Single Target Label:** We first present our results for the single target label case. Figure 5 compares the accuracies of the backdoored model $M_{bd}$ and the clean model $M$ -on the clean testing dataset-. As the figure shows, our backdoored models achieve the same performance as the clean models for both the MNIST and CelebA datasets, i.e., 99% for MNIST and 70% for CelebA. For the CIFAR-10 dataset, there is a slight drop in performance, which is less than 2%. This shows that our Random Backdoor technique can implement a perfectly functioning backdoor, i.e., the backdoor success rate of $M_{bd}$ is 100% on the backdoored testing dataset, with a negligible utility loss.

To visualize the output of our Random Backdoor technique, we first randomly sample 8 images from the MNIST dataset, and then use the Random Backdoor technique to construct triggers for them. Finally, we add these triggers to the images using the backdoor adding function $A$, and show the result in Figure 6a. As the figure shows, the triggers all look distinctly different and are located at different locations as expected.

**Multiple Target Labels:** Second, we present our results for the multiple target label case. To recap, we consider all possible labels for this case. For instance, for the MNIST dataset, we consider all digits from 0 to 9 as our target labels. We train our Random Backdoor models for the multiple target label case. To recap, we consider all possible labels for this case. For instance, for the MNIST dataset, we consider all digits from 0 to 9 as our target labels.

We use a similar evaluation setting to the single target label case, with the following exception. To evaluate the performance of the backdoored model $M_{bd}$ with multiple target labels, we construct a backdoored testing dataset for each target label by generating and adding triggers to the clean testing dataset. In other words, we use all images in the testing dataset to evaluate all possible labels.

Similar to the single target label case, we focus on the accuracy on the clean testing dataset, since the backdoor success rate for all models on the backdoored testing datasets are approximately 100% for all target labels.

We use the clean testing datasets to evaluate the backdoored model’s ($M_{bd}$) utility, i.e., we compare the performance of the backdoored model $M_{bd}$ with the clean model $M$ in Figure 7. As the figure shows, using our Random Backdoor technique, we are able to train backdoored models that achieve similar performance as the clean models for all datasets. For instance, for the CIFAR-10 dataset, our Random Backdoor technique achieves 92% accuracy, which is very similar to the accuracy of the clean model (92.4%). For the CelebA dataset, the Random Backdoor technique achieves a slightly (about 2%) better performance than the clean model. We believe this is due to the regularization effect of the Random Backdoor technique. Finally, for the MNIST dataset, both models achieve a similar performance with just 1% difference between the clean model (99%) and the backdoored one (98%).

To visualize the output of our Random Backdoor technique on multiple target labels, we construct triggers for all possible labels in the CIFAR-10 dataset, and use $A$ to add them to a randomly sampled image from the CIFAR-10 clean testing dataset. Figure 8a shows the image with different triggers. The different patterns and locations used for the different target labels can be clearly demonstrated in Figure 8a. For instance, comparing the location of the trigger for the first and sixth images, the triggers are in the same horizontal position but a different vertical position, as previously illustrated in Figure 2.

Moreover, we further visualize in Figure 9a the dynamic behavior of the triggers generated by our Random Backdoor technique. Without loss of generality, we generate triggers for...
the backdoor adding function \( \mathcal{M}_{bd} \) for all possible labels set as target labels, but we visualize the triggers for a single label to show the dynamic behaviour of our Random Backdoor technique with respect to the triggers’ pattern and locations. As Figure 9a shows, the generated triggers have different patterns and locations for the same target label, which achieves our desired dynamic behavior.

D. Backdoor Generating Network (BaN)

Next, we evaluate our BaN technique. We follow the same evaluation settings for the Random Backdoor technique, except with respect to how the triggers are generated. We train our BaN model and generate the triggers as mentioned in Section III-B.

Single Target Label: Similar to the Random Backdoor, the BaN technique achieves perfect backdoor success rate with a negligible utility loss. Figure 5 compares the performance of the backdoored models trained using the BaN technique, with the clean models on the clean testing dataset. As Figure 5 shows, our BaN trained backdoored models achieve 99%, 92.4% and 70% accuracy on the MNIST, CIFAR-10, and CelebA datasets, respectively, which is the same performance of the clean models.

We visualize the BaN generated triggers using the MNIST dataset in Figure 6b. To construct the figure, we use the BaN to generate multiple triggers -for the target label 0-, then we add them on a set of randomly sampled MNIST images using the backdoor adding function \( \mathcal{A} \).

The generated triggers look very similar as shown in Figure 6b. This behaviour is expected as the MNIST dataset is simple, and the BaN technique does not have any explicit loss to enforce the network to generate different triggers. However, to show the flexibility of our approach, we increase the randomness of the BaN network by simply adding one more dropout layer after the last layer, to avoid the overfitting of the BaN model to a unique pattern. We show the results of the BaN model with higher randomness in Figure 6c. The resulting model still achieves the same performance, i.e., 99% accuracy on the clean data and 100% backdoor success rate, but as the figure shows the triggers look significantly different. This again shows that our framework can easily adapt to the requirements of an adversary.

These results together with the results of the Random Backdoor (Section IV-C) clearly show the effectiveness of both of our proposed techniques, for the single target label case. They are both able to achieve almost the same accuracy of a clean model, with a 100% working backdoor, for a single target label.

Multiple Target Labels: Similar to the single target label case, we focus on the backdoored models’ performance on the testing clean dataset, as our BaN backdoored models achieve a perfect accuracy on the backdoored testing dataset, i.e., the backdoor success rate for all datasets is approximately 100% for all target labels.

We compare the performance of the BaN backdoored models with the performance of the clean models on the clean testing dataset in Figure 7. Our BaN backdoored models are able to achieve almost the same accuracy as the clean model for all datasets, as can be shown in Figure 7. For instance, for the CIFAR-10 dataset, our BaN achieves 92.1% accuracy, which is only 0.3% less than the performance of the clean model (92.4%). Similar to the Random Backdoor backdoored models, our BaN backdoored models achieve a marginally better performance for the CelebA dataset. More concretely, our BaN backdoored models trained for the CelebA dataset achieve about 2% better performance than the clean model, on the clean testing dataset. We also believe this improvement is due to the regularization effect of the BaN technique. Finally, for the MNIST dataset, our BaN backdoored models achieve strong performance on the clean testing dataset (98%), which is just 1% lower than the performance of the clean models (99%).

Similar to the Random Backdoor, we visualize the results of the BaN backdoored models with two figures. The first (Figure 8b) shows the different triggers for the different target labels on the same CIFAR-10 image, and the second (Figure 9b) shows the different triggers for the same target label (plane) on randomly sampled CIFAR-10 images. As both figures show, the BaN generated triggers achieves the dynamic behaviour in both the location and patterns. For instance, for the same target label (Figure 9b), the patterns of the triggers look significantly different and the locations vary vertically. Similarly, for different target labels (Figure 8b), both the pattern and location of triggers are significantly different.

E. conditional Backdoor Generating Network (c-BaN)

Next, we evaluate our conditional Backdoor Generating Network (c-BaN) technique. For the c-BaN technique, we only consider the multiple target labels case, since there is only a single label so the conditional addition to the BaN technique is not needed. In other words, for the single target label case, the c-BaN technique will be the same as the BaN technique.

We follow a similar setup as introduced for the BaN technique in Section IV-D, with the exception on how to train the backdoored model \( \mathcal{M}_{bd} \) and generate the triggers. We follow Section III-C to train the backdoored model and generate the triggers. For the set of possible locations \( \mathcal{K} \), we use four possible locations.

We compare the performance of the c-BaN with the other two techniques in addition to the clean model. All of our three dynamic backdoor techniques achieve an almost perfect backdoor success rate on the backdoored testing datasets, hence similar to the previous sections, we focus on the performance on the clean testing datasets.

Figure 7 compares the accuracy of the backdoored and clean models using the clean testing dataset, for all of our three dynamic backdoor techniques. As the figure shows, all of our dynamic backdoored models have similar performance
as the clean models. For instance, for the CIFAR-10 dataset, our c-BaN, BaN and Random Backdoor achieves 92%, 92.1% and 92% accuracy, respectively, which is very similar to the accuracy of the clean model (92.4%). Also for the MNIST dataset, all models achieve very similar performance with no difference between the clean and c-BaN models (99%) and 1% difference between the BaN and Random Backdoor (98%), and the clean model.

Similar to the previous two techniques, we visualize the dynamic behaviour of the c-BaN backdoored models, first, by generating triggers for all possible labels and adding them on a CIFAR-10 image in Figure 8c. More generally, Figure 8 shows the visualization of all three dynamic backdoor techniques in the same settings, i.e., backdooring a single image to all possible labels. As the figure shows, the Random Backdoor Figure 8a has the most random patterns, which is expected as they are sampled from a uniform distribution. The figure also shows the different triggers' patterns and locations used for the different techniques. For instance, each target label in the Random Backdoor (Figure 8a) and BaN (Figure 8b) techniques have a unique (horizontal) location, unlike the c-BaN (Figure 8c) generated triggers, which different target labels can share the same locations, as can be shown for example in the first, second, and ninth images. To recap, both the Random Backdoor and BaN techniques split the location set $\mathcal{K}$ on all target labels, such that no two labels share a location, unlike the c-BaN technique which does not have this limitation.

Second, we visualize the dynamic behaviour of our techniques, by generating triggers for the same target label 5 (plane) and adding them to a set of randomly sampled CIFAR-10 images. Figure 9 compares the visualization of our three different dynamic backdoor techniques in this setting. To make it clear, we train the backdoor model $M_{bd}$ for all possible labels set as target labels, but we plot for a single label to visualize how different the triggers look like for each target label. As the figure shows, the Random Backdoor (Figure 9a) and BaN (Figure 9b) generated triggers can move vertically, however, they have a fixed position horizontally as mentioned in Section III-A and illustrated in Figure 2. The c-BaN (Figure 9c) triggers also show different locations. However, the locations of these triggers are more distant and can be shared for different target labels, unlike the other two techniques. Finally, the figure also shows that all triggers have different patterns for our techniques for the same target label, which achieves our targeted dynamic behavior concerning the patterns and locations of the triggers.

F. Evaluating Against Current State-Of-The-Art Defenses

We now evaluate our attacks against the current state-of-the-art backdoor defenses. Backdoor defenses can be classified into the following two categories, data-based defenses and model-based defenses. On one hand, data-based defenses focus on identifying if a given input is clean or contains a trigger. On the other hand, model-based defenses focus on identifying if a given model is clean or backdoored.

We first evaluate our attacks against model-based defenses, then we evaluate them against data-based ones.

Model-based Defense: We evaluate all of our dynamic backdoor techniques in the multiple target label case against two of the current state-of-the-art model-based defenses, namely, Neural Cleanse [47] and ABS [21].

We start by evaluating the ABS defense. We use the CIFAR-10 dataset to evaluate this defense, since it is the only supported dataset by the published defense model. As expected, running the ABS model against our dynamic backdoored ones does not result in detecting any backdoor for all of our models.
Next, we evaluate the current state-of-the-art data-based defense, namely, STRIP [10]. STRIP tries to identify if a given input is clean or contains a trigger. It works by creating multiple images from the input image by fusing them with multiple clean images one at a time. Then STRIP applies all fused images to the target model and calculates the entropy of predicted labels. Backdoored inputs tend to have lower entropy compared to the clean ones.

We use all of our three datasets to evaluate the c-BaN models against this defense. First, we scale the patterns by half while training the backdoored models, to make them more susceptible to changes. Second, for the MNIST dataset, we move the possible locations to the middle of the image to overlap with the image content, since the value of the MNIST images at the corners are always 0. All trained scaled backdoored models achieve similar performance to the non-scaled backdoored models.

Our backdoored models successfully flatten the distribution of entropy for the backdoored data, for a subset of target labels. In other words, the distribution of entropy for our backdoored data overlaps with the distributions of entropy of the clean data. This subset of target labels makes picking a threshold to identify backdoored from clean data impossible without increasing the false positive rate, i.e., various clean images will be detected as backdoored ones. We visualize the entropy of our best performing labels against the STRIP defense in Figure 10.

Moreover, since our dynamic backdoors can generate dynamic triggers for the same input and target label. The adversary can keep querying the target model while backdooring the input with a fresh generated trigger until the model accepts it. These results against the data and model-based defenses show the effectiveness of our dynamic backdoor attacks, and opens the door for designing backdoor detection systems that work against both static and dynamic backdoors, which we plan for future work.

G. Evaluating Different Hyperparameters

We now evaluate the effect of different hyperparameters for our dynamic backdooring techniques. We start by evaluating the percentage of the backdoored data needed to implement a dynamic backdoor into the model. Then, we evaluate the effect of increasing the size of the location set \( K \). Finally, we evaluate the size of the trigger and the possibility of making it more transparent, i.e., instead of replacing the original values in the input with the backdoor, we fuse them.

Proportion of the Backdoored Data: We start by evaluating the percentage of backdoored data needed to implement a dynamic backdoor in the model. We use the MNIST dataset and the c-BaN technique to perform the evaluation. First, we construct different training datasets with different percentages of backdoored data. More concretely, we try all proportions from 10% to 50%, with a step of 10. 10% means that 10% of the data is backdoored, and 90% is clean. Our results show that using 30% is already enough to get a perfectly working dynamic backdoor, i.e., the model has a similar performance like a clean model on the clean dataset (99% accuracy), and 100% backdoor success rate on the backdoored dataset. For any percentage below 30%, the accuracy of the model on clean data is still the same, however, the performance on the backdoored dataset starts degrading.

Number of Locations: Second, we explore the effect of increasing the size of the set of possible locations \( (K) \) for...
the c-BaN technique. We use the CIFAR-10 dataset to train a backdoored model using the c-BaN technique, but with more than double the size of $K$, i.e., 8 locations. The trained model achieves similar performance on the clean (92%) and backdoored (100%) datasets. We then doubled the size again to have 16 possible locations in $K$, and the model again achieves the same results on both clean and backdoored datasets. We repeat the experiment with the CelebA datasets and achieve similar results, i.e., the performance of the model with a larger set of possible locations is similar to the previously reported one. However, when we try to completely remove the location set $K$ and consider all possible locations with a sliding window, the performance on both clean and backdoored datasets significantly dropped.

**Trigger Size:** Next, we evaluate the effect of the trigger size on our c-BaN technique using the MNIST dataset. We train different models with the c-BaN technique, while setting the trigger size from 1 to 6. We define the trigger size to be the width and height of the trigger. For instance, a trigger size of 3 means that the trigger is $3 \times 3$ pixels.

We calculate the accuracy on the clean and backdoored testing datasets for each trigger size, and show our results in Figure 12. Our results show that the smaller the trigger, the harder it is for the model to implement the backdoor behaviour. Moreover, small triggers confuse the model, which results in reducing the model’s utility. As Figure 12 shows, a trigger with the size 5 achieves a perfect accuracy (100%) on the backdoored testing dataset, while preserving the accuracy on the clean testing dataset (99%).

**Transparency of the Triggers:** Finally, we evaluate the effect of making the trigger more transparent. More specifically, we change the backdoor adding function $A$ to apply a weighted sum, instead of replacing the original input’s values. Abstractly, we define the weighted sum of the trigger and the image as:

$$x_{bd} = s \cdot t + (1 - s) \cdot x$$

where $s$ is the scale controlling the transparency rate, $x$ is the input and $t$ is the trigger. We implement this weighted sum only at the location of the trigger, while maintaining the remaining of the input unchanged.

We use the MNIST dataset and c-BaN technique to evaluate the scale from 0 to 1 with a step of 0.25. Figure 11 visualizes the effect of varying the scale when adding a trigger to an input.

Our results show that our technique can achieve the same performance on both the clean (99%) and backdoored (100%) testing datasets, when setting the scale to 0.5 or higher. However, when the scale is set below 0.5, the performance starts degrading on the backdoored dataset but stays the same on the clean dataset. We repeat the same experiments for the CelebA dataset and find similar results.

### V. Related Works

In this section, we discuss some of the related work. We start with current state-of-the-art backdoor attacks. Then we discuss the defenses against backdoor attacks, and finally mention other attacks against machine learning models.

**Backdoor Attacks:** Gu et al. [12] introduce BadNets, the first backdoor attack on machine learning models. BadNets uses the MNIST dataset and a square-like trigger with a fixed location, to show the applicability of the backdoor attacks in the machine learning settings. Liu et al. [22] later propose a more advanced backdooring technique, namely the Trojan attack. They simplify the threat model of BadNets by eliminating the need for Trojan attack to access the training data. The Trojan attack reverse-engineers the target model to synthesize training data. Next, it generates the trigger in a way that maximizes the activation functions of the target model’s internal neurons related to the target label. In other words, the Trojan attack reverse-engineers a trigger and training data to retrain/update the model and implement the backdoor.

The main difference between these two attacks (BadNets and Trojan attacks) and our work is that both attacks only consider static backdoors in terms of triggers’ pattern and location. Our work extends the backdoor attacks to consider dynamic patterns and locations of the triggers.

**Defenses Against Backdoor Attacks:** Defenses against backdoor attacks can be classified into model-based defenses and data-based defenses.
First, model-based defenses try to find if a given model contains a backdoor or not. For instance, Wang et al. [47] propose Neural Cleanse (NC), a backdoor defense method based on reverse engineering. For each output label, NC tries to generate the smallest trigger, which converts the output of all inputs applied with this trigger to that label. NC then uses anomaly detection to find if any of the generated triggers are actually a backdoor or not. Later, Liu et al. [21] propose another model-based defense, namely, ABS. ABS detects if a target model contains a backdoor or not, by analyzing the behaviour of the target model’s inner neurons when introducing different levels of stimulation.

Second, data-based defenses try to find if a given input is clean or backdoored. For instance, Gao et al. [10] propose STRIP, a backdoor defense method based on manipulating the input, to find out if it is backdoored or not. More concretely, STRIP fuses the input with multiple clean data, one at a time. Then it queries the target model with the generated inputs, and calculate the entropy of the output labels. Backdoored inputs tend to have lower entropy than the clean ones.

**Attacks Against Machine Learning:** Poisoning attack [17], [42], [5] is another training time attack, in which the adversary manipulates the training data to compromise the target model. For instance, the adversary can change the ground truth for a subset of the training data to manipulate the decision boundary, or more generally influence the model’s behavior. Shafahi et al. [38] further introduce the clean label poisoning attack. Instead of changing labels, the clean label poisoning attack allows the adversary to modify the training data itself to manipulate the behaviour of the target model.

Another class of ML attacks is the adversarial examples. Adversarial examples share some similarities with the backdoor attacks. In this setting, the adversary aims to trick a target classifier into misclassifying a data point by adding controlled noise to it. Multiple works have explored the privacy and security risks of adversarial examples [32], [45], [6], [20], [43], [33], [48]. Other works explore the adversarial example’s potentials in preserving the user’s privacy in multiple domains [30], [18], [51], [19]. The main difference between adversarial examples and backdoor attacks is that backdoor attacks are done in training time, while adversarial examples are done after the model is trained and without changing any of the model’s parameters.

Beside the above, there are multiple other types of attacks against machine learning models, such as membership inference [39], [16], [13], [34], [35], [24], [14], [25], [50], [27], [41], [37], [28], model stealing [44], [31], [46], model inversion [8], [7], [15], property inference [9], [26], and dataset reconstruction [36].

**VI. Conclusion**

The tremendous progress of machine learning has lead to its adoption in multiple critical real-world applications, such as authentication and autonomous driving systems. However, it has been shown that ML models are vulnerable to various types of security and privacy attacks. In this paper, we focus on backdoor attack where an adversary manipulates the training of the model to intentionally misclassify any input with an added trigger.

Current backdoor attacks only consider static triggers in terms of patterns and locations. In this work, we propose the first set of dynamic backdoor attack, where the trigger can have multiple patterns and locations. To this end, we propose three different techniques.

Our first technique Random Backdoor samples triggers from a uniform distribution and place them at a random location of an input. For the second technique, i.e., Backdoor Generating Network (BaN), we propose a novel generative network to construct triggers. Finally, we introduce conditional Backdoor Generating Network (c-BaN) to generate label specific triggers.

We evaluate our techniques using three benchmark datasets. Evaluation shows that all our techniques can achieve almost a perfect backdoor success rate while preserving the model’s utility. Moreover, we show that our techniques successfully bypass state-of-the-art defense mechanisms against backdoor attacks.

**References**
