
Maximizing Broadcast Coverage Using Range Control for Dense Wireless Networks

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Future Building Blocks

- Small complete systems
 - CPU, memory, stable storage, wireless network
- Low cost
 - □ \$10
- Low power
 - Devices draw power from the environment
- Small size
 - 1cm³
- Berkeley Mote is a prototype

Motivation

- Future density
 - At \$10, tag most objects
 - At \$1 tag everything
 - Lab inventory shows 530 objects in
- Heavy use of broadcast
 - Localization (E.g. Ad-hoc Positioning system)
 - Routing (E.g. Dynamic Source Routing)
 - Management (STEM)
 - Time Synchronization

A Common Pattern

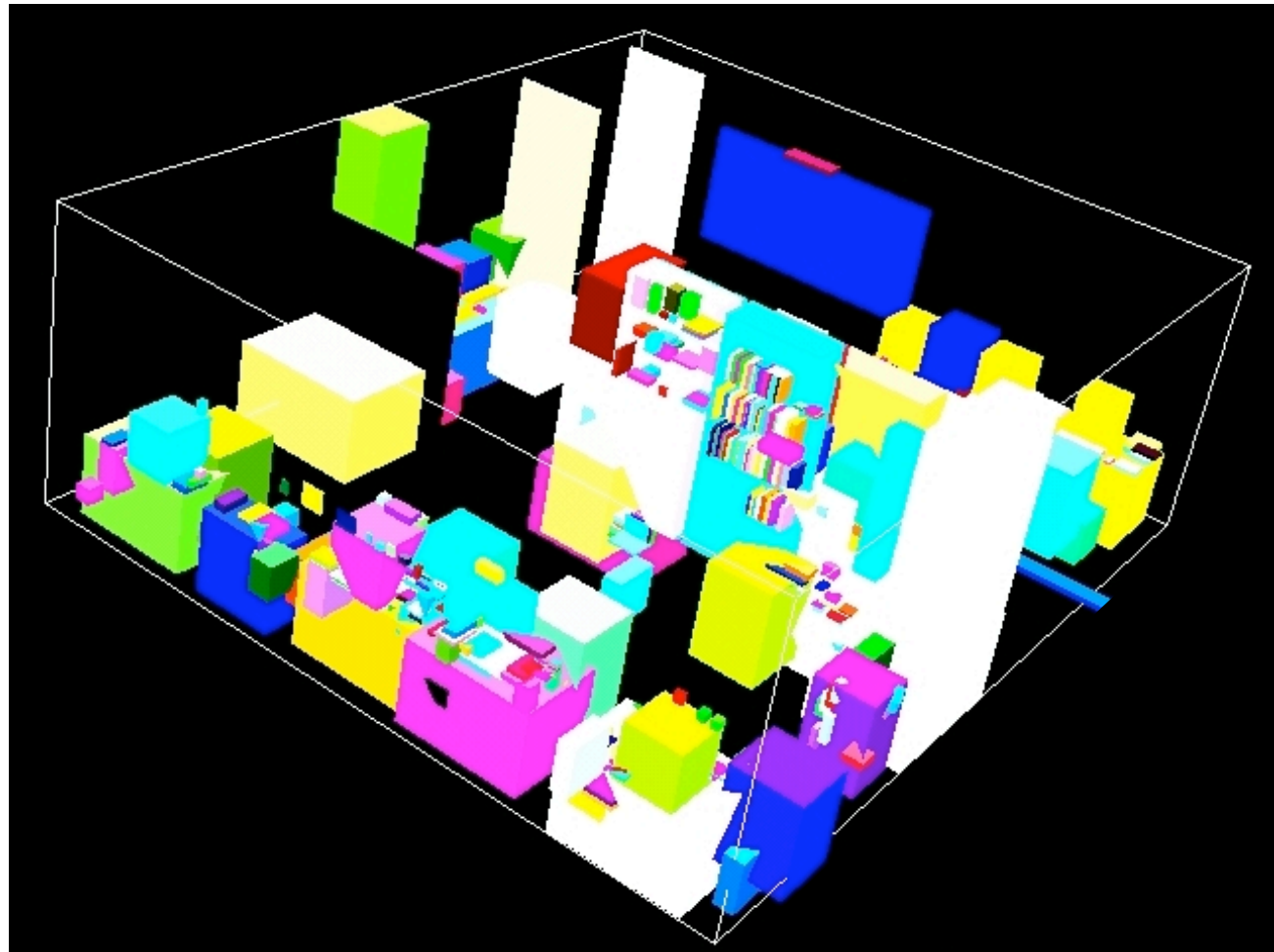
```
Foreach (time-interval) {  
    Broadcast(some state);  
    Wait(time-interval){  
        Collect neighbour responses;  
    }  
    Do something;  
}
```

Spatial Inventory

PANIC Lab

528 objects

137m³



Range Control

Problem Statement

- Broadcast, density and CSMA lead to channel collapse
 - Unicast better limits resource using feedback (e.g. RTS/CTS)
- Challenge: maximize number of receivers of a broadcast packet
 - Distributed
 - Low overhead
 - No Extra protocol messages, complex exchanges
 - Fair

Assumptions

- Ad-Hoc Style
- Few channels available
 - E.g. 802.11b -> 11 channels
 - not 1000's
- CMTSA control for broadcasts
- Predictable mapping between range and power

Strategy

- Sharing Strategies:
 - Rate control
 - Channel control
 - Range/power control
- Our approach
 - Passive observation of local density and sending rate to set range to maximize broadcast coverage
 - Set power control to conform to range setting

Implementation Strategy

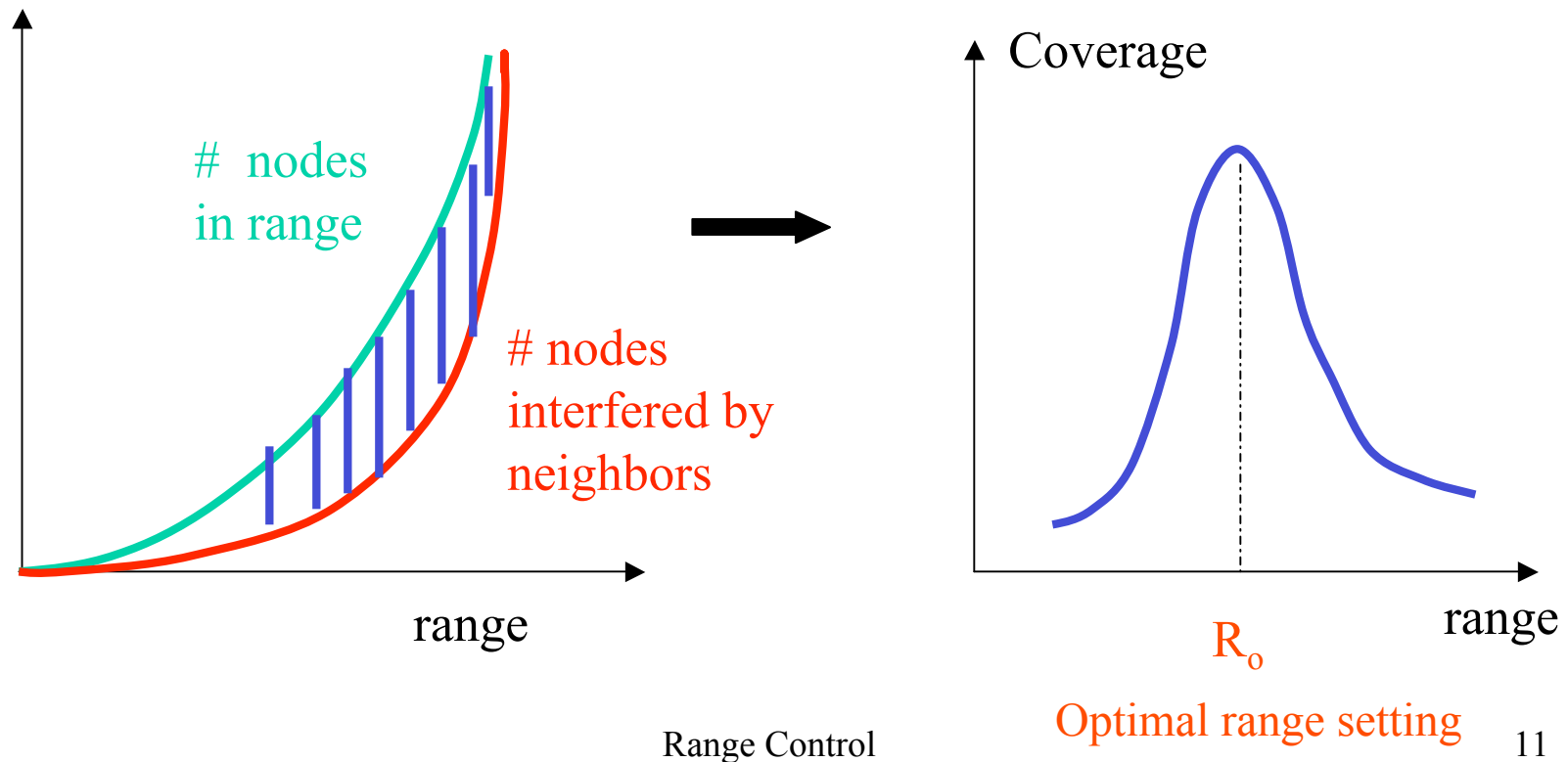
Layer 4	transport
Layer 3	network
Layer 2	LLC
	Ranging & Power
	MAC
Layer 1	Physical

Outline

- Introduction and motivation
- Analytic model of optimal Range
- Application of the model to the distributed algorithm
- Simulation Results
- Future Work and Conclusions

Finding Optimal Coverage

$$\text{Coverage} = \# \text{ nodes in range} - \# \text{ nodes experiencing interference}$$



Analytic Modeling

Want:

- Set range to R_o , which has the highest **expected** coverage.

How:

- Derive a general formula for expected coverage in specific environments and radius setting

$$\square C = f(\text{env}, \text{radius})$$

- optimal radius is the one which maximize C value

$$\square \frac{df}{dr} (r=R_o) = 0$$

Analytic Model Basics

- **Node distribution:** multi-dimension poisson distribution: λ_s
- **Transmission rate:** poisson packet arrival: λ_p
- **Packet Length:** constant size (transmission time T)
- **MAC protocol:** CSMA
- **Transmission range:** Nodes use the same radius R .
- **Wireless model:**
 - Nodes within range R to the transmitter are able to hear the packet.
 - More than one transmitter within distance R to the receiver will corrupt all the packets at the receiver.
- **Goal :** Derive the optimal radius setting R_0 for specific environment $\{\lambda_s, \lambda_p, T\}$

Modeling Inaccuracy

- Mismatch with practical physical transmission model

$$\frac{\frac{P_i}{|X_i - X_j|^\alpha}}{N + \sum_{\substack{k \in \mathcal{T} \\ k \neq i}} \frac{P_k}{|X_k - X_j|^\alpha}} \geq \beta.$$

- No accounting for unicast traffic
- Analytic model inaccuracy:
 - Assume all nodes use the same range
 - Assume transmission times arrive as a poisson process (really CSMA)
 - Geometric approximation

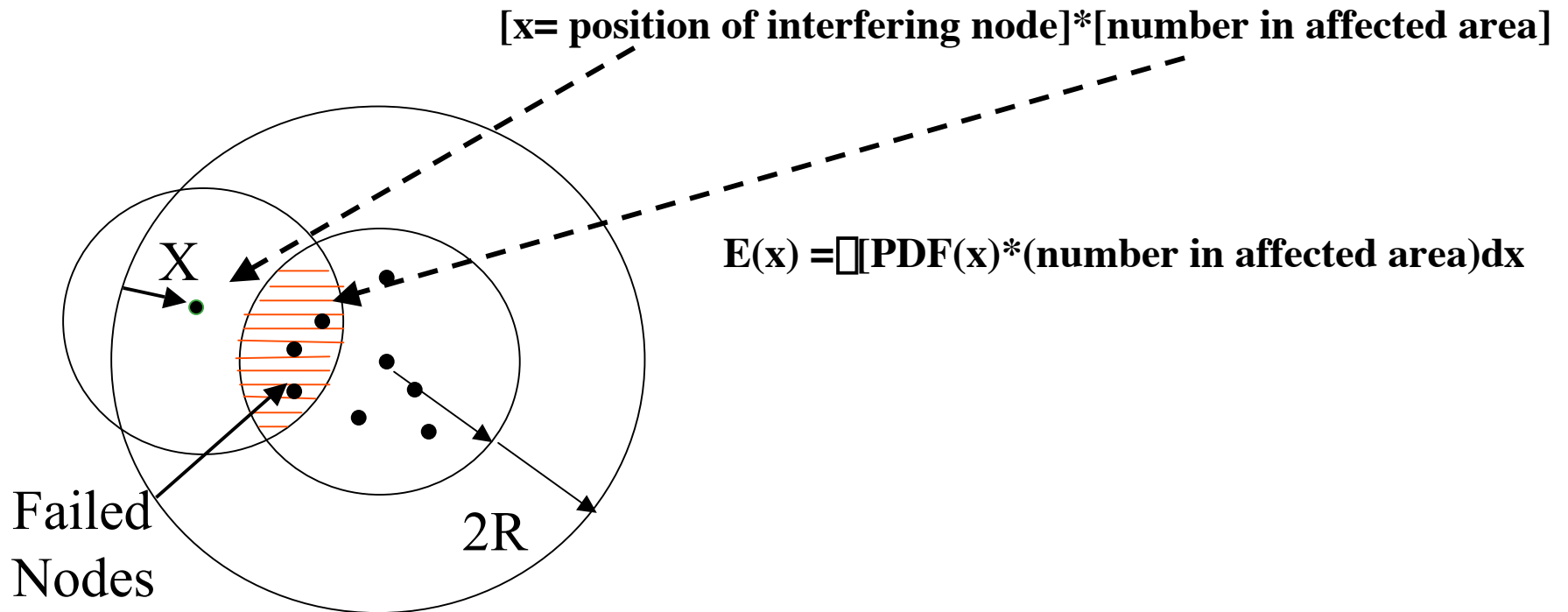
Packet Arrival Simplification

- CSMA makes node transmissions dependent
 - Basically slows down the transmission rate
- Simplification #1
 - assume nodes out of range still follow INDEPENDENT poisson transmission with density
- Effect: Conservative to R_0
 - over-estimates the interference coming from neighbors
 - error on side of smaller R : prevent channel collapse over more coverage

Geometric Approach

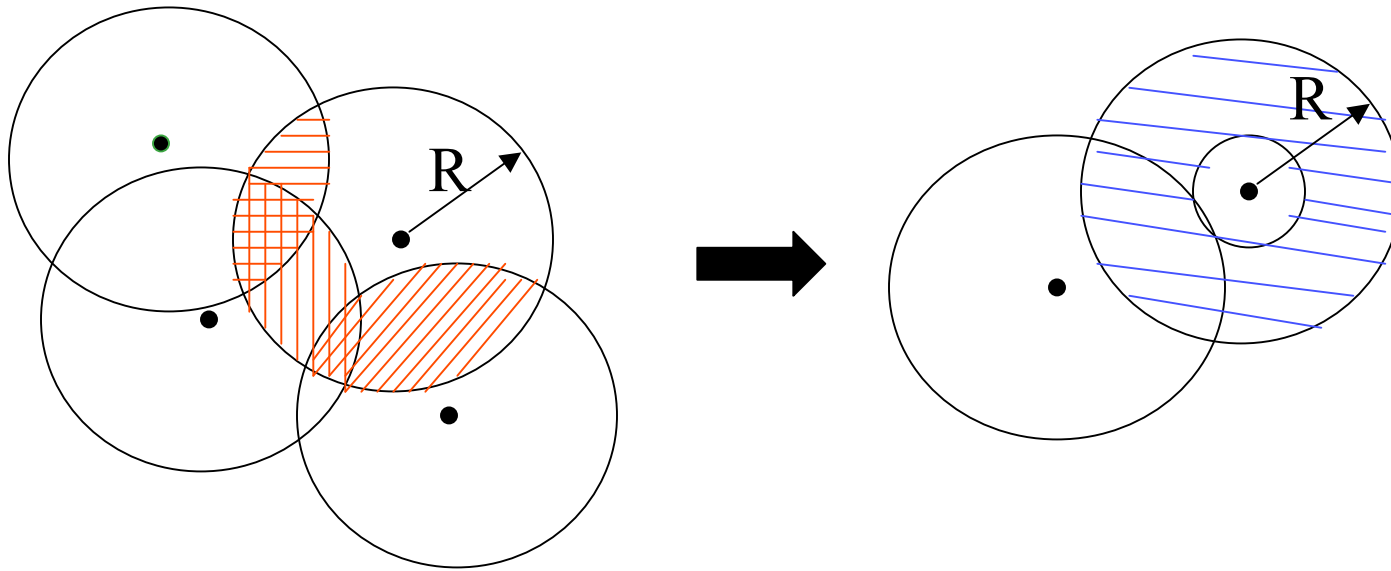
- Expected coverage of a packet =
[Nodes in range]-[losses from hidden terminals]
- Random variable, X , is distance of closest interfering node
 - Compute CDF, i.e. $P(x < X)$
- Find expected number of failed nodes given at each point in PDF
- Subtract expected number failed from total nodes in range

Geometric Approach



Geometric Simplification (#2)

Computing expected failing area is difficult



- Torus approximates overlapping intersecting circles(spheres)
i.e. blue approximates area red.
- This simplification is also conservative to R_0

Expected Coverage

$$\text{CDF}(x) = e^{-\lambda_s * \pi * ((2R - x)^2 - R^2) * (1 - e^{-\lambda_p * 2T})}$$

$$E(C) = \lambda_s * (\pi * R^2) - \int_0^R [\lambda_s * \pi * (R^2 - (R - x)^2) * P(z \leq x \leq z + dz)] dz$$

Expected nodes
in range

Expected number failed

Problem:

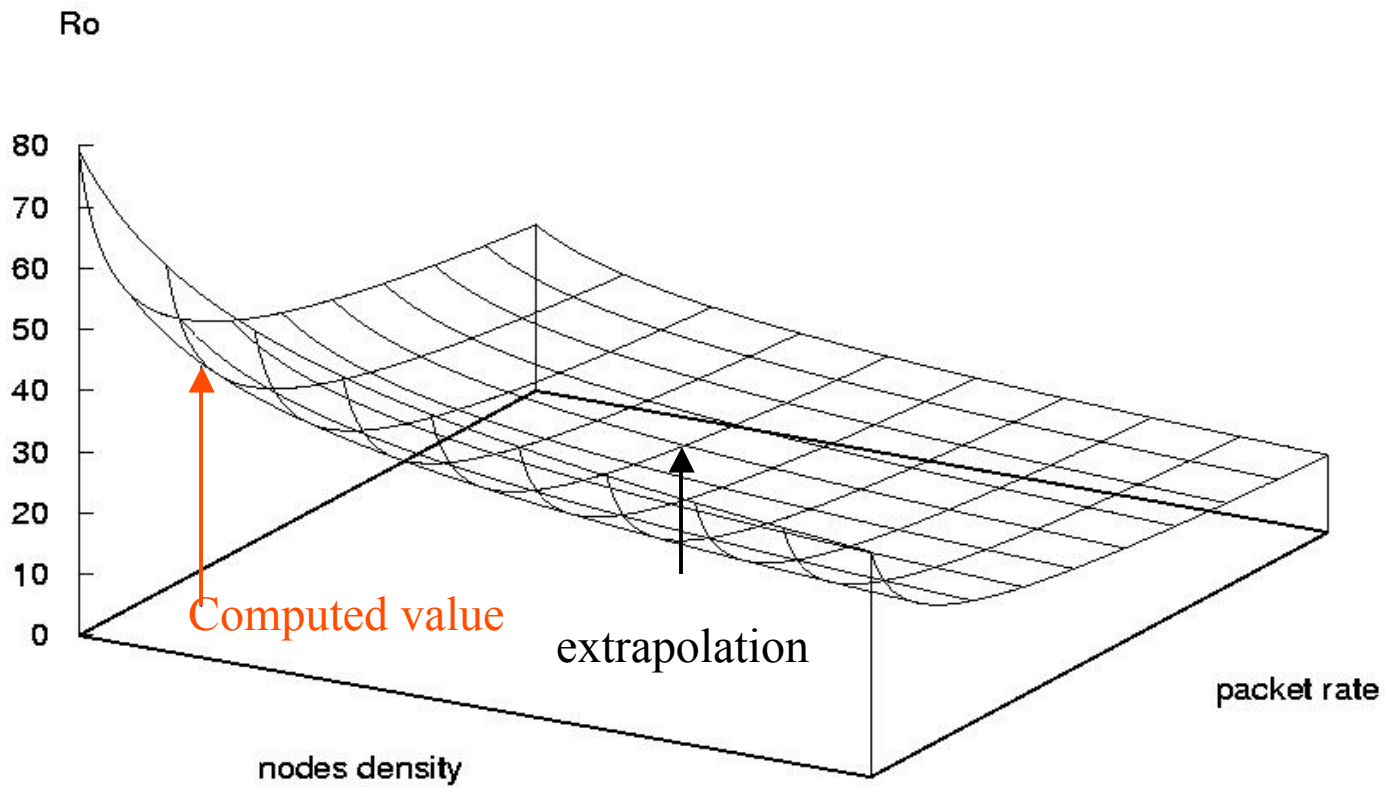
- It's not a closed form formula – can't solve the integral
 - Can't solve for R_0 directly

Extrapolate to find optimal

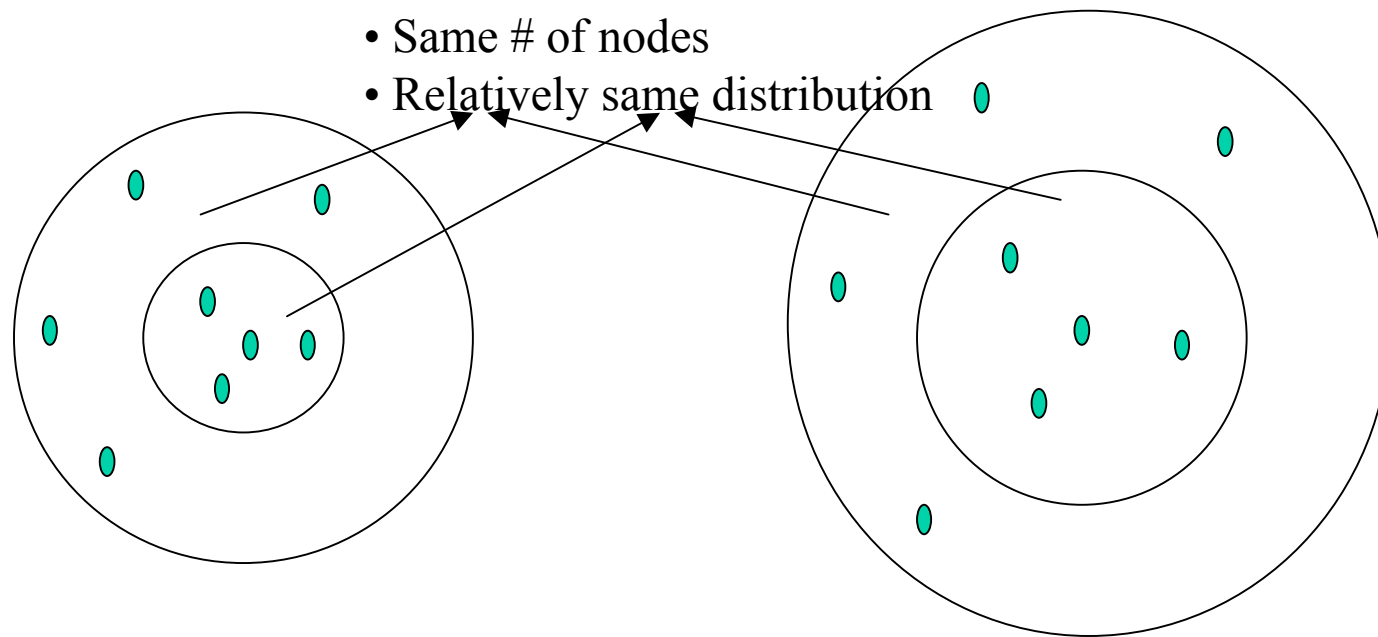
- Solve R_0 for the in a specific setting $\{\lambda_s, \lambda_p, T\}$ numerically (e.g. maple).
- Assume T is stable – constant packet size.
- If we can extrapolate R_0 for any arbitrary setting of environments from a known optimal, then we can still apply our idea.

$$\square \quad \{\lambda_s, \lambda_p, R_0\} \longrightarrow \{\lambda'_s, \lambda'_p, R'_0\}$$

Using extrapolations



Extrapolation I: Constant Shape



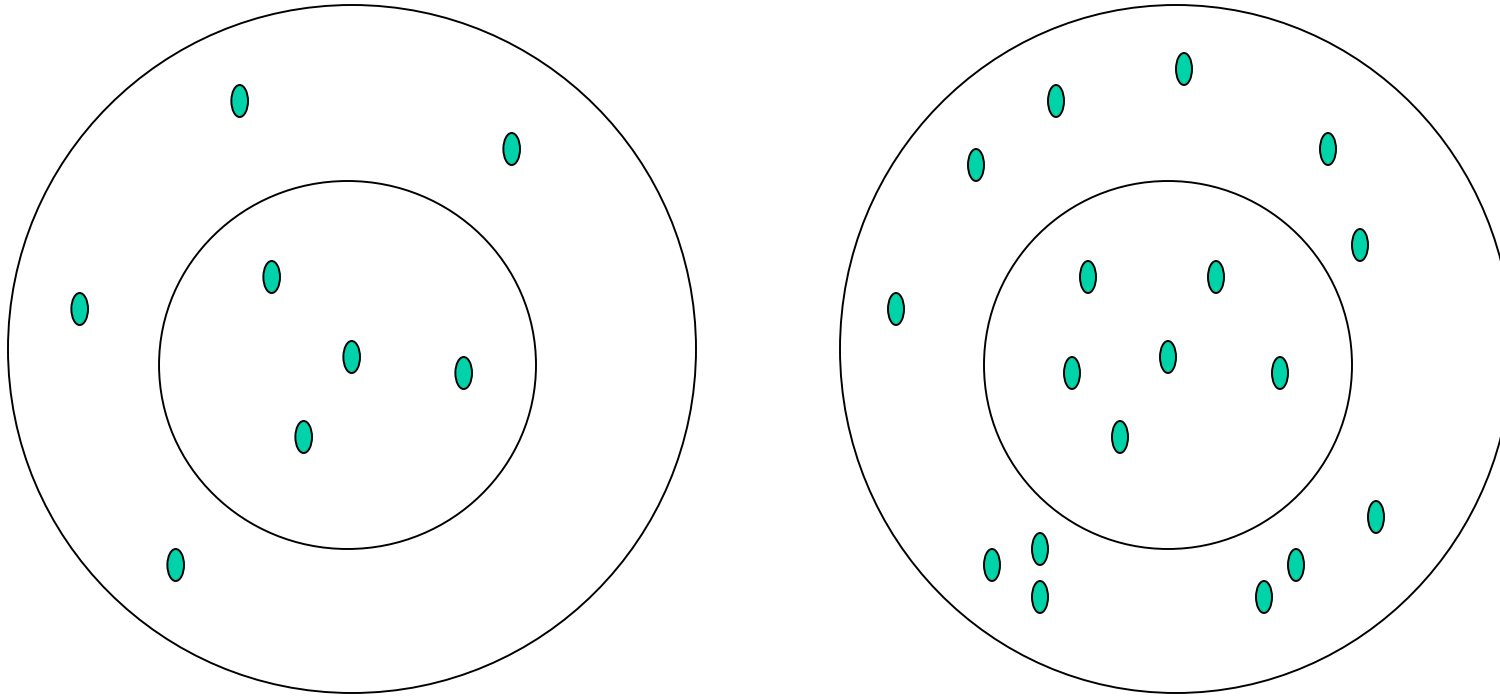
Same rate, different density

Alter R to obtain same # of expected nodes in circle and torus

\Rightarrow Same expected coverage.

$$\lambda_{p1} = \lambda_{p2}, \lambda_{s1} * R_1^2 = \lambda_{s2} * R_2^2 \Rightarrow E(C_1) = E(C_2)$$

Extrapolation II: Constant Packet Volume



Fewer nodes sending frequently is equivalent to more nodes sending infrequently

$$\lambda_{s1} * (1 - e^{-\lambda_{p1} * 2T}) = \lambda_{s2} * (1 - e^{-\lambda_{p2} * 2T}), R_1 = R_2 \Rightarrow \frac{E(C_1)}{E(C_2)} = \frac{\lambda_{s1}}{\lambda_{s2}}$$

Range Control

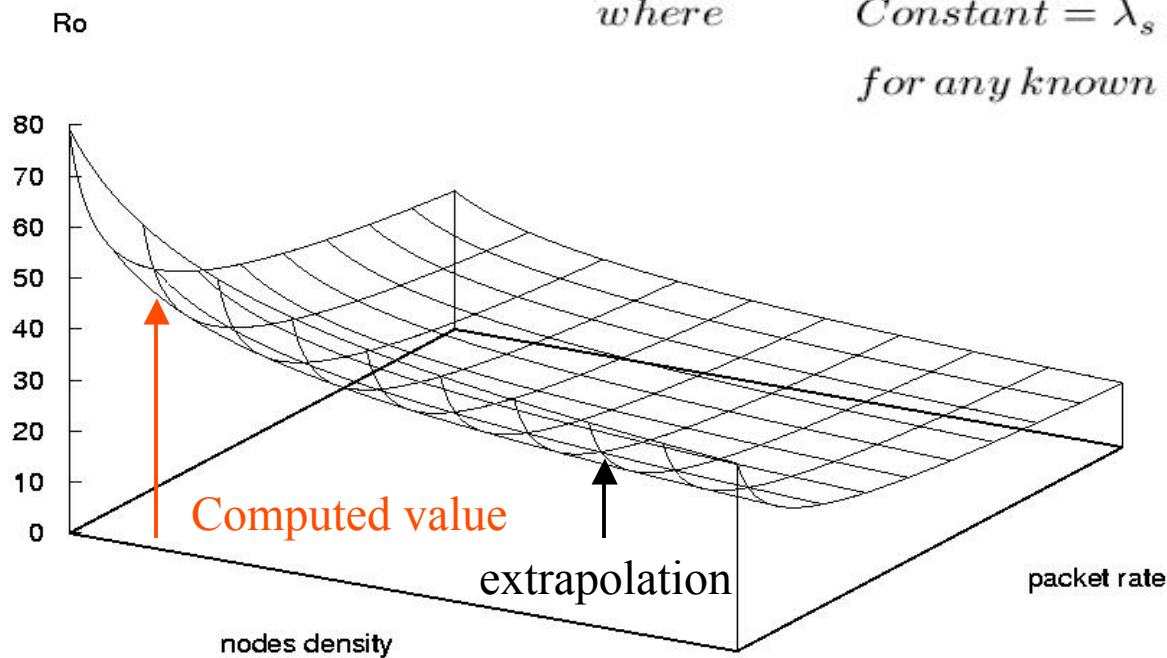
Extrapolation accuracy

- Extrapolation I (spatial) is exact
- Extrapolation II (network volume) is approximate
 - assume nodes' transmissions are still independent in spite of CSMA
 - More nodes, more collisions
 - Higher density, less collisions
 - Not clear which effect is stronger

Combining Extrapolations

$$R_o = \sqrt{\frac{\text{Constant}}{\lambda_s * (1 - e^{-\lambda_p * 2T})}}$$

where $\text{Constant} = \lambda'_s * (1 - e^{-\lambda'_p * 2T}) * R_o'^2$
for any known set $\{\lambda'_s, \lambda'_p, R_o'\}$



Verification of extrapolations

Node density (nodes/m ³)	Packet rate (pkts/sec)	R _o extrapolation error
0.002 – 0.01	0.4 – 2.0	11% - 20%

Conservative assumptions:

- constant fudge factor of +5% "safe"

The Distributed Algorithm

- Over an **adjustment interval**
 - (20 broadcasts)
 - Collect neighbor list
 - Neighbors expire if not refreshed for 5 intervals
 - Average send rate
- Compute density at end of interval
 - Use assume spheres
- Set R_0 for the next interval
- If only it were that easy ...

Handling Imprecision

- Analytic model assumes perfect information
- Approaches to handling imprecision:
 - Warm up period
 - Overload/underload disambiguation
 - Outlier consideration
 - Minimize impact of outliers
 - Longer-range push and pull messages
 - Insure accurate density estimates
 - Accounts for non-uniform densities

Initialization/warm up

- Initial guess of R
- Wait at least one interval
- Adjust R until there are sufficient neighbors (N)
- If the channel is in overload:
 - Reduce R to cover half the volume
- If not enough expected nodes based on density (underload):
 - Increase R to double volume
 - Expected N = $\pi \frac{C_o}{(1 - e^{-\lambda p^2 T})}$
- Once neighbor list is $\geq N$, set R_0
 - continue to set each interval based only on last density and rate

Outliers

- Keep outliers from impacting local density estimate
- Use median
 - Sort neighbours based on distance
 - Keep a running density computation
 - Take median density

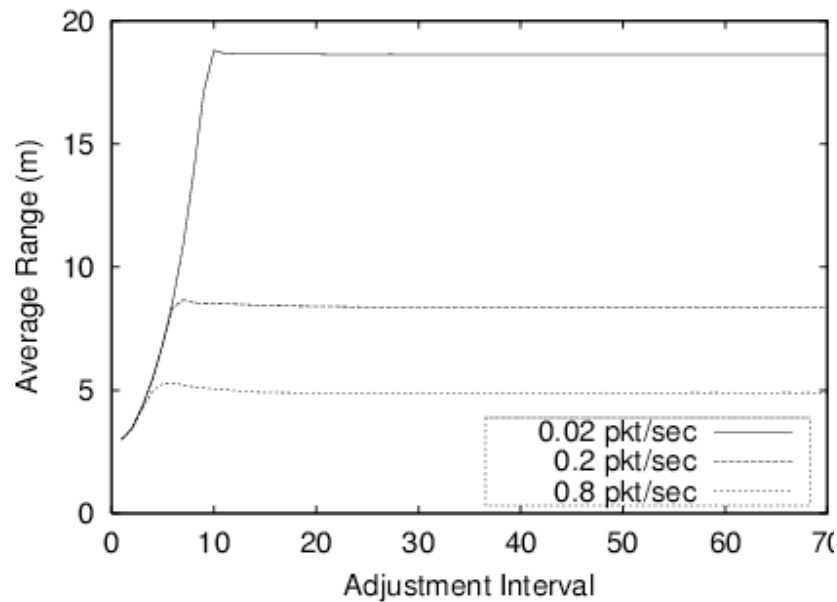
Increasing accuracy with extended range messages

- **Pull and Push** messages
 - just extend range of a normal broadcast
- **Pulls account for hidden terminals**
 - Density estimate should include hidden terminals
 - Range set to 2x volume
- **Pushes account for asymmetric ranges**
 - Nodes should account for all affected nodes
 - Range set to distance of furthest node
 - Accounts for non-uniform densities
- **2% of broadcasts are push or pulls**
 - Neighbors from push/pull expire after 25 intervals

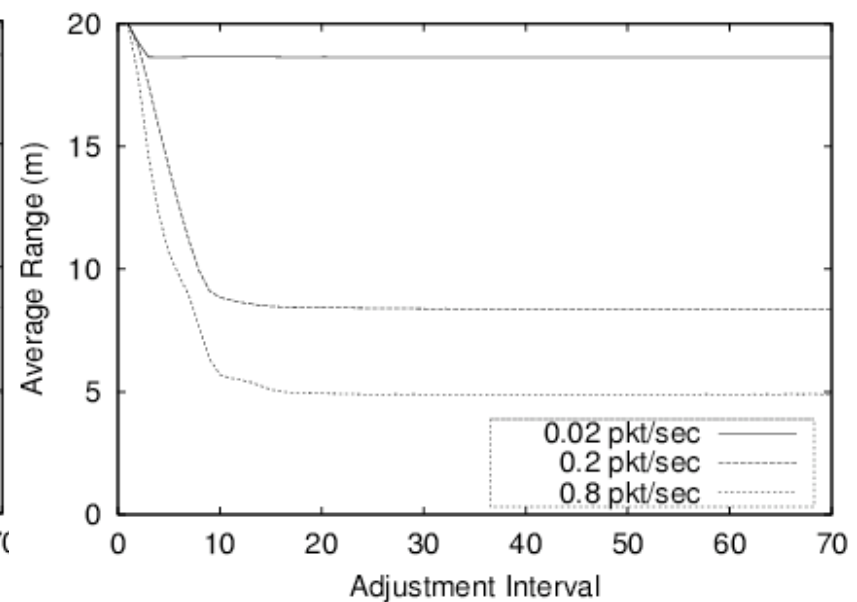
Simulation Results

- Simulated 3-D environment
 - Simulations of 5K nodes, 100m³
- Tested robustness to initial conditions
 - Ranges too high, too low, random
 - Observe convergence speed, final ranges and coverage
- Tested robustness to non-uniform density
 - Used topology based on lab inventory
- Observed impact on a higher-level protocol
 - A hop-by-hop localization protocol

Convergence speed

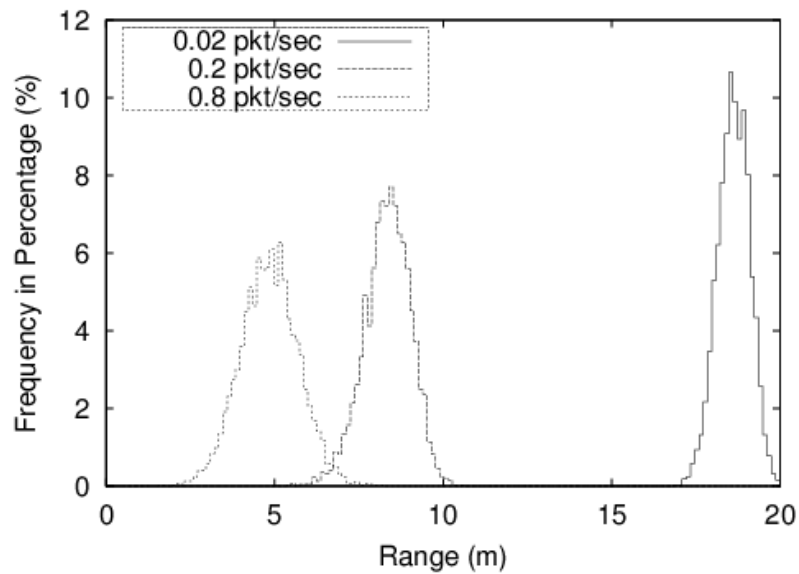


Initial $R=3$

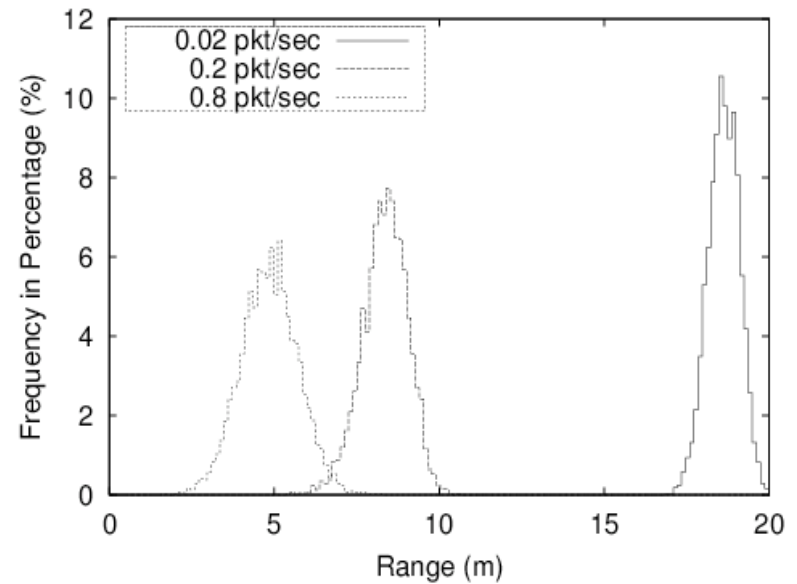


Initial $R=20$

Robustness to Initial Ranges

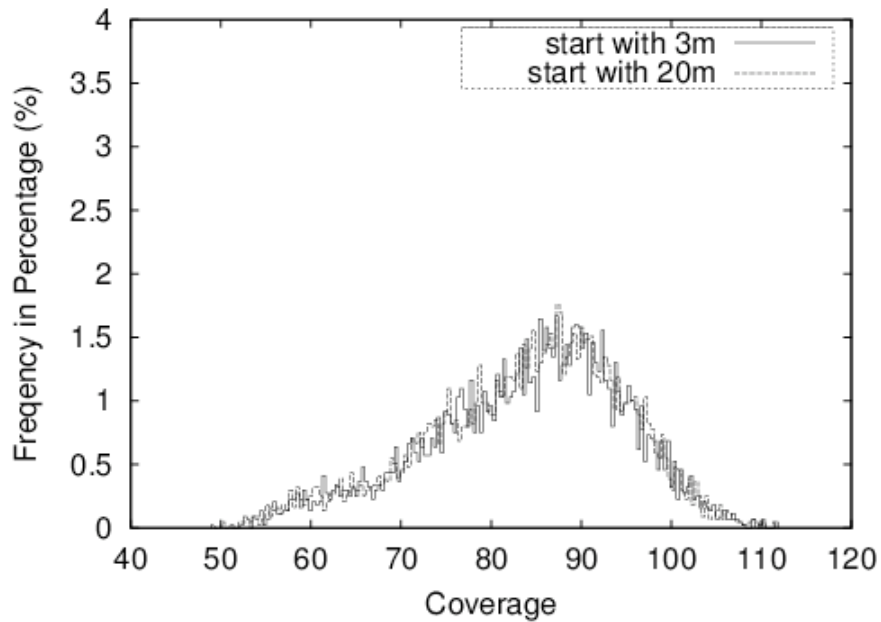


Initial R=3

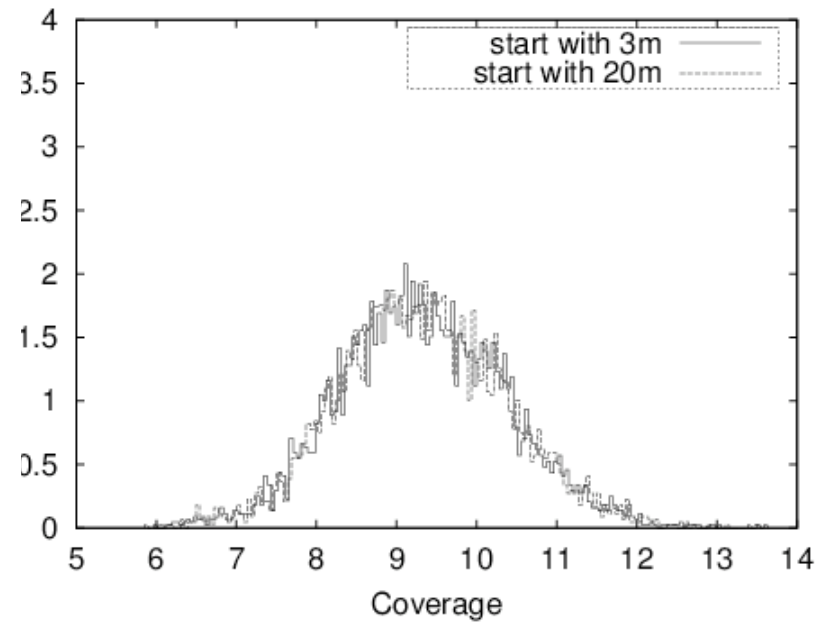


Initial R=20

Final Coverages

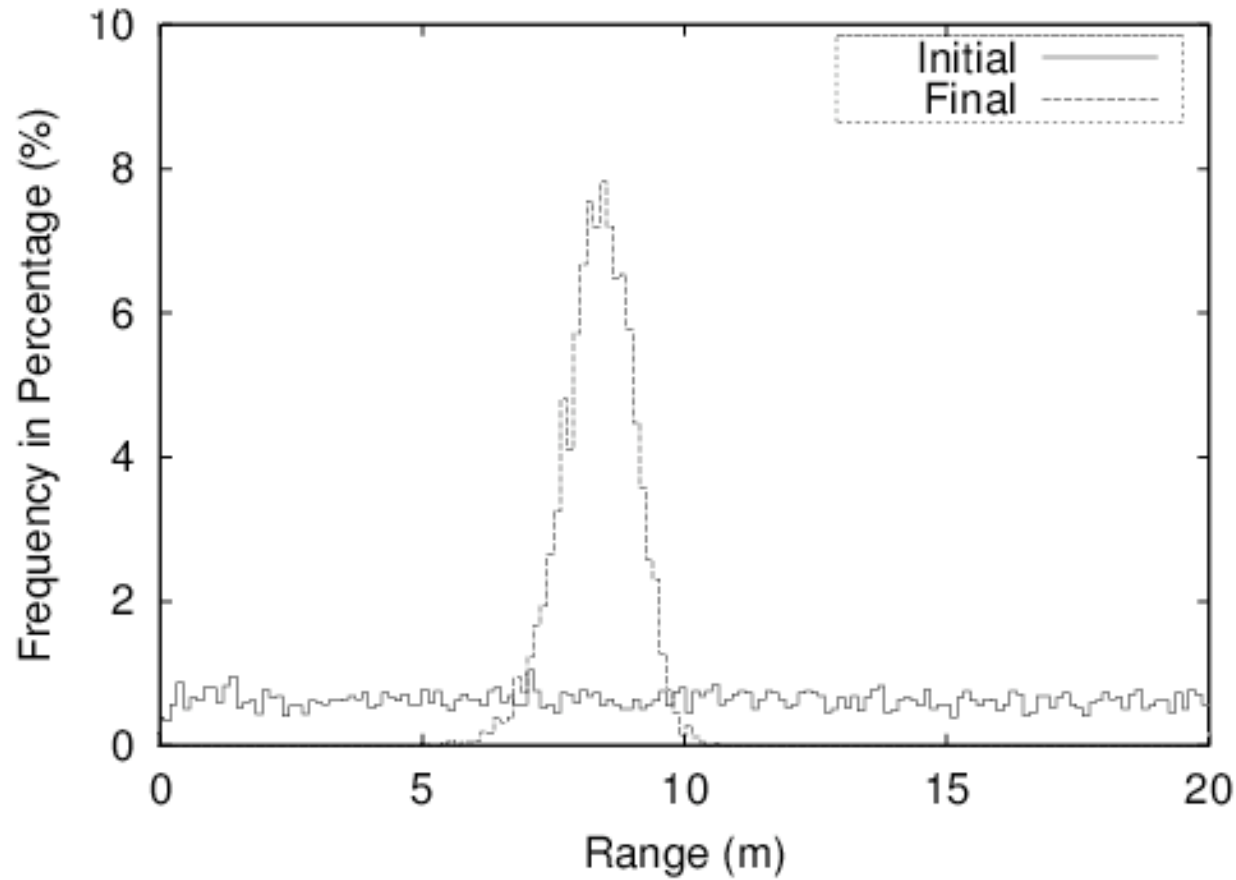


Arrival Rate = 0.02 pkts/s

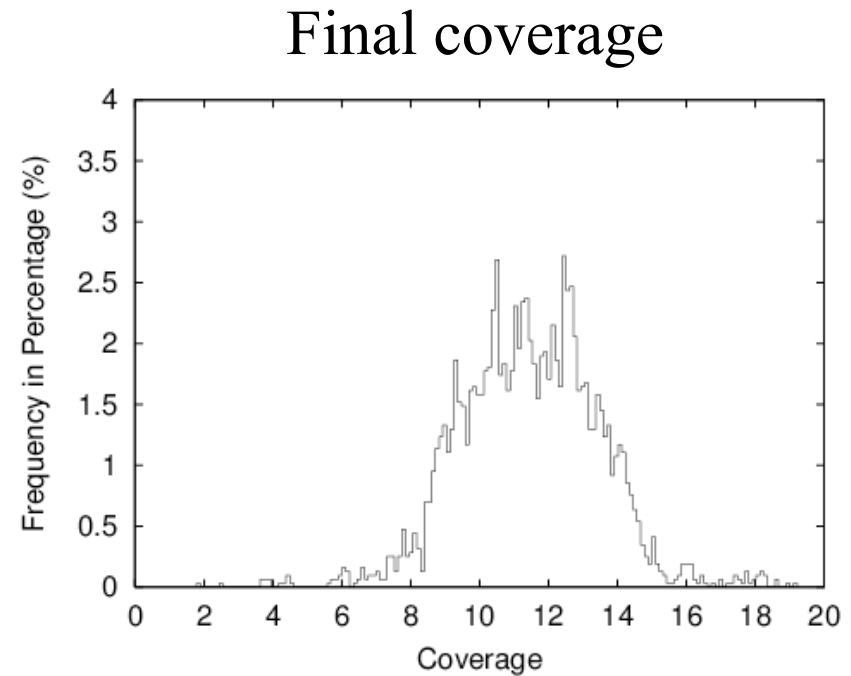
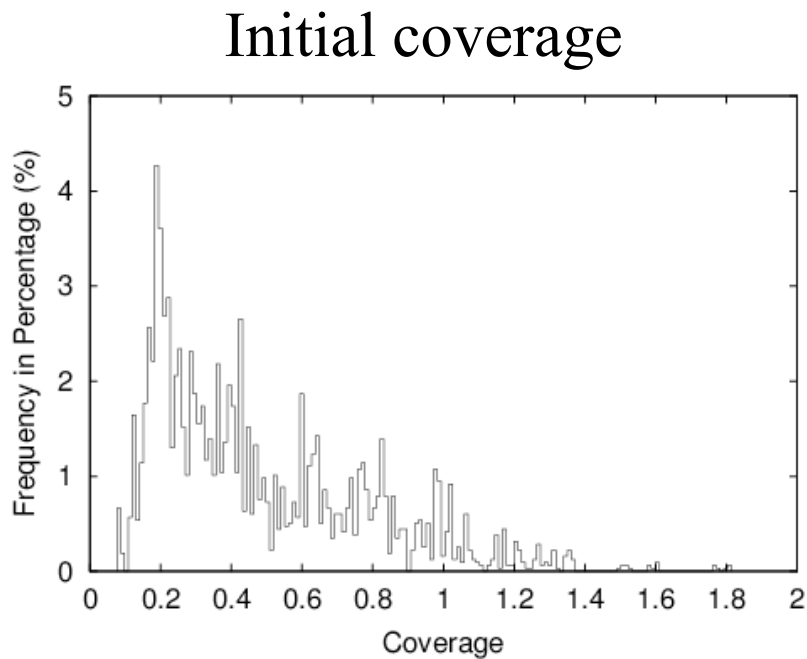


Arrival Rate = 0.2 pkts/s

Robustness to Random Initial Ranges



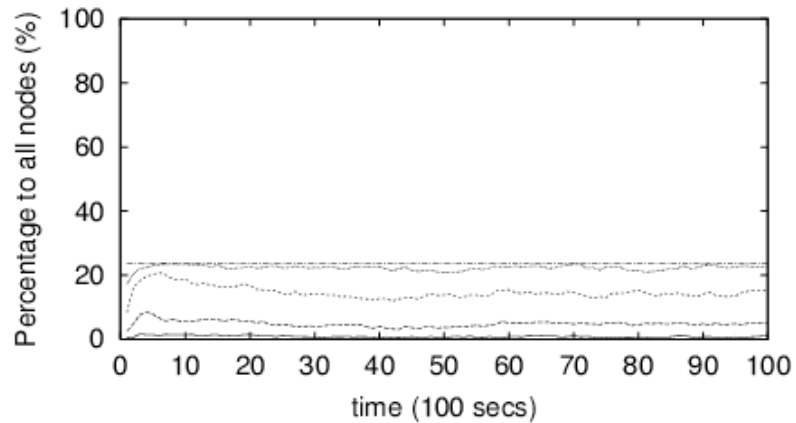
Non-uniform networks



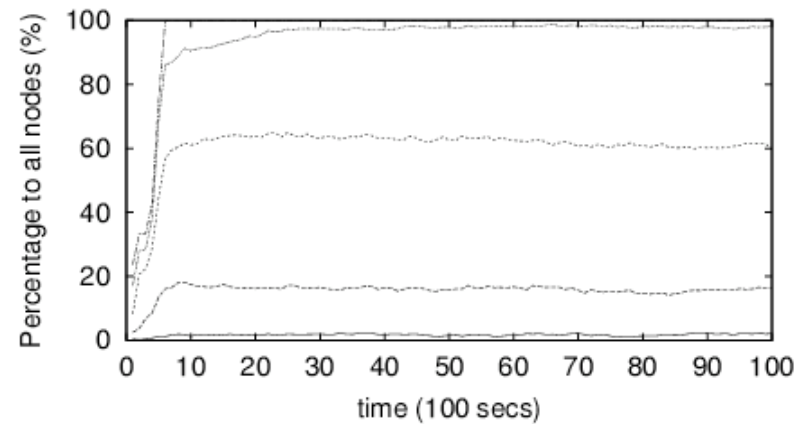
3100 nodes (lab replicated 6x),

Impact on a localization protocol

No Range Control



Using Range Control



Future work and Conclusions

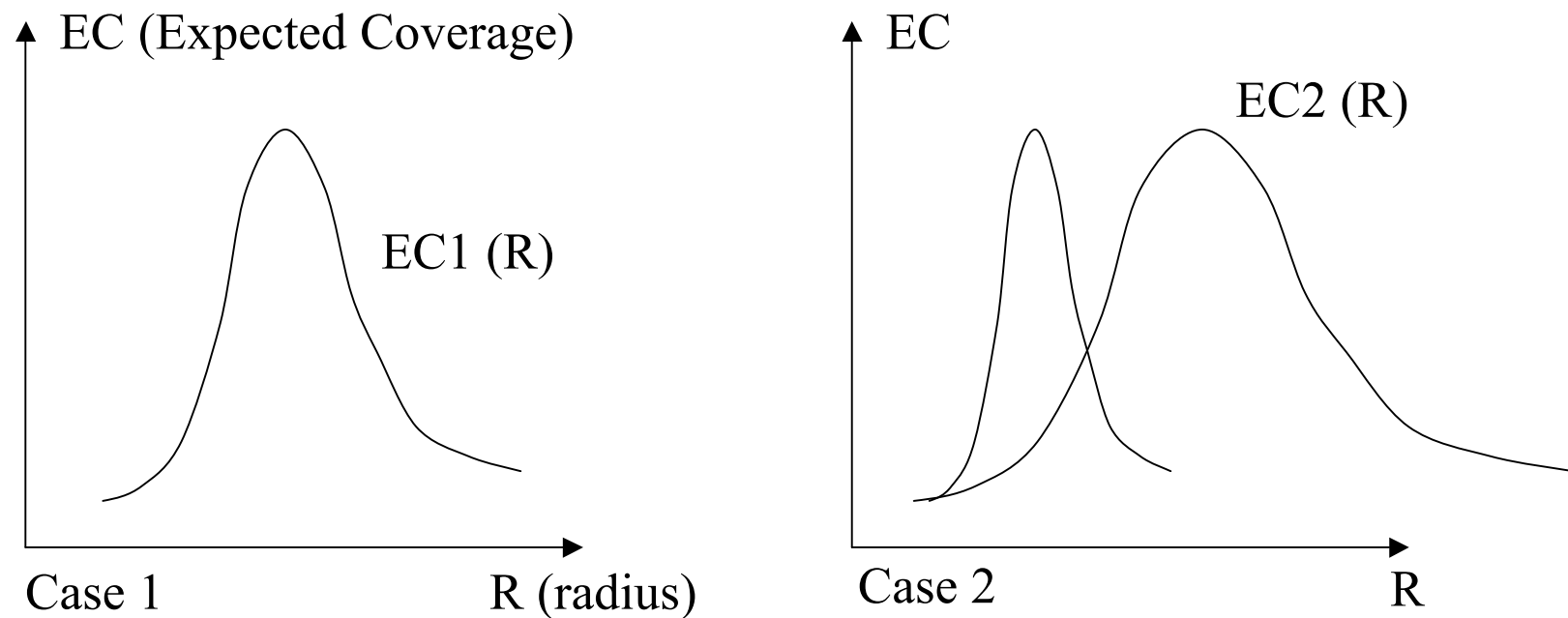
- Range control promising approach
- Continue validations:
 - Floor and building-wide simulations
 - Dynamic Network (join and leave)
 - Real implementations
 - 802.11 and motes
- Need more higher-level protocols
- Need realistic traffic patterns
 - Chicken and egg problem

Backup slides

- These slides are for questions and answers

Extrapolation based on rule I

$$\lambda_{p1} = \lambda_{p2}, \lambda_{s1} * R_1^2 = \lambda_{s2} * R_2^2 \Rightarrow E(C_1) = E(C_2)$$

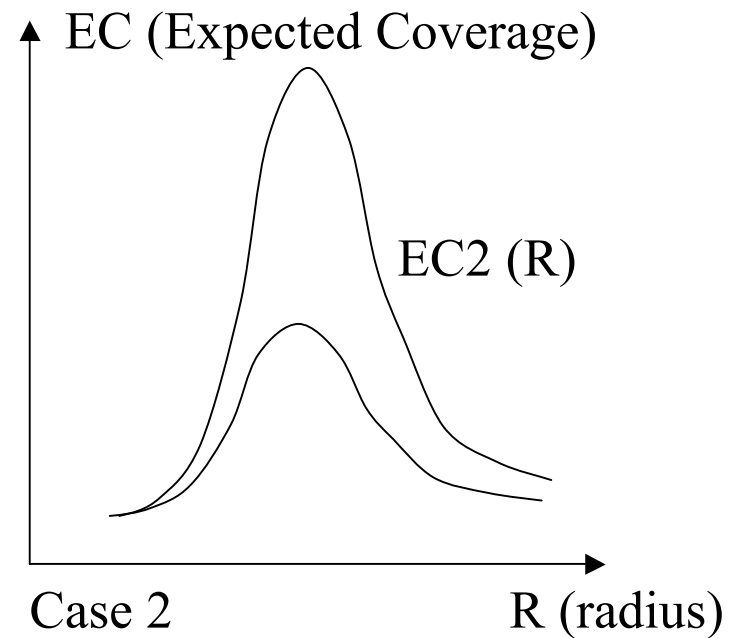
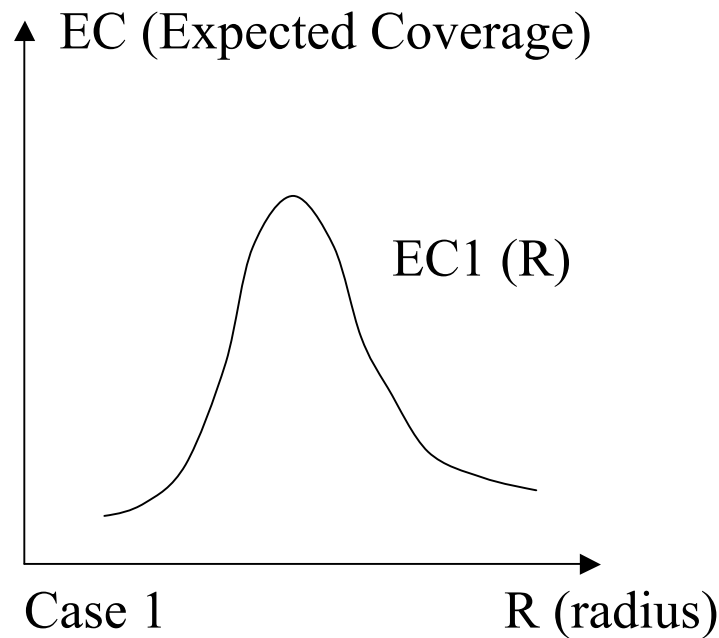


$$\lambda_{p1} = \lambda_{p2} \Rightarrow EC2(R) = EC1\left(\sqrt{\frac{\lambda_{s2}}{\lambda_{s1}}} * R\right)$$

$$\lambda_p = \lambda'_p \Rightarrow R'_o = \sqrt{\frac{\lambda_s * R_o^2}{\lambda'_s}}$$

Extrapolation based on rule II

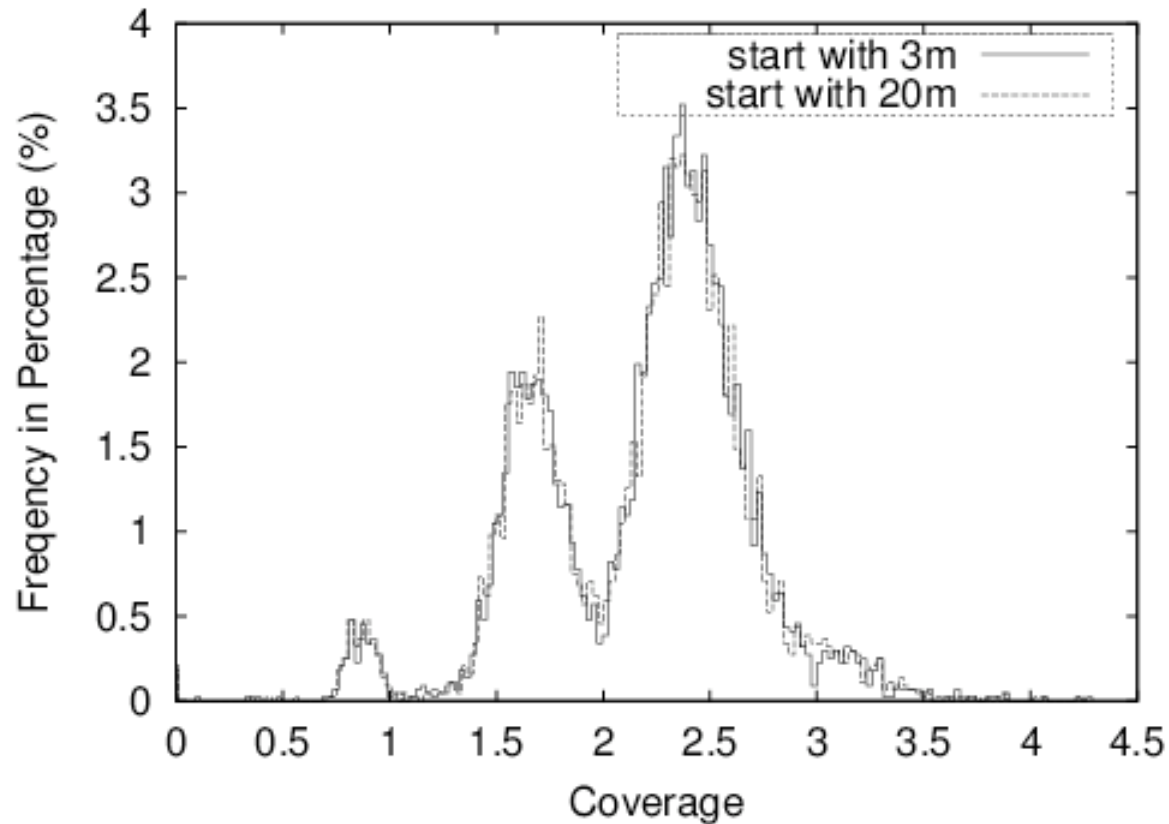
$$\lambda_{s1} * (1 - e^{-\lambda_{p1} * 2T}) = \lambda_{s2} * (1 - e^{-\lambda_{p2} * 2T}), R_1 = R_2 \Rightarrow \frac{E(C_1)}{E(C_2)} = \frac{\lambda_{s1}}{\lambda_{s2}}$$



$$\lambda_{s1} * (1 - e^{-\lambda_{p1} * 2T}) = \lambda_{s2} * (1 - e^{-\lambda_{p2} * 2T}) \Rightarrow EC2(R) = \frac{\lambda_{s2}}{\lambda_{s1}} * EC1(R)$$

$$\lambda_s * (1 - e^{-\lambda_p * 2T}) = \lambda'_s * (1 - e^{-\lambda'_p * 2T}) \Rightarrow R'_o = R_o$$

Uniform Coverage



Arrivale Rate = 0.8 pskts/sec