

# Distributed Systems

## 24. Cryptographic Systems: A Brief Introduction

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# Cryptography $\neq$ Security

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Cryptography may be a component of a secure system

Adding cryptography may not make a system secure

# Cryptography: what is it good for?

- **Confidentiality**
  - others cannot read contents of the message
- **Authentication**
  - determine origin of message
- **Integrity**
  - verify that message has not been modified
- **Nonrepudiation**
  - sender should not be able to falsely deny that a message was sent

# Confidentiality

# Encryption

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Plaintext (cleartext) message  $P$

Encryption  $E(P)$

Produces Ciphertext,  $C = E(P)$

Decryption,  $P = D(C)$

Cipher = cryptographic algorithm

# Terms: types of ciphers

- **Symmetric** algorithm

- Shared key

$$C = E_k(P) \quad P = D_k(C)$$

- Key length → difficulty of attack

- **Public key** algorithm

- Key pair: **private key (k)** & a shared **public key (K)**

$$C = E_k(P) \quad P = D_k(C)$$

$$C = E_K(P) \quad P = D_k(C)$$

# Key distribution

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Secure key distribution is the biggest problem with symmetric cryptography

# Distributing Keys

- **Manual: pre-shared keys**
  - Initial configuration, out of band (send via USB key, recite, ...)
- **Trusted third party**
  - Knows all keys
  - Alice creates a **session key**
  - Encrypts it with her key – sends to Trent
  - Trent decrypts it and sends it to Bob
  - Alternatively: Trent creates a session key – encrypts it for Alice & for Bob
- **Public key cryptography**
  - Alice encrypts a message with Bob's public key
  - Only Bob can decrypt
- **Diffie-Hellman**
- **Hybrid cryptosystems**



# Diffie-Hellman Key Exchange

## Key distribution algorithm

- First algorithm to use public/private “keys”

- Not public key encryption

- Uses a **one-way function**

Based on difficulty of computing discrete logarithms in a finite field compared with ease of calculating exponentiation

- Compute

**common key** =  $f(\text{your\_private\_key}, \text{their\_public\_key})$

- Eavesdroppers cannot compute this

# Hybrid Cryptosystems

- **Session key**: randomly-generated key for one communication session
- Use a **public key algorithm** to send the session key
- Use a **symmetric algorithm** to encrypt data with the session key

Public key algorithms are almost never used to encrypt messages

- MUCH slower; vulnerable to *chosen-plaintext attacks*
- RSA-2048 approximately 55x slower to encrypt and 2,000x slower to decrypt than AES-256

# Message Integrity

# Hash functions

- **Cryptographic hash function** (also known as a **digest**)
  - Input: arbitrary data
  - Output: fixed-length bit string
- Properties of a cryptographic hash,  $H=\text{hash}(M)$ :
  - **One-way function**
    - Given  $H$ , it should be difficult to compute  $M$
  - **Collision resistant**
    - Given  $H$ , it should be difficult to find  $M'$ , such that  $H=\text{hash}(M')$
    - For a hash of length  $L$ , a perfect hash would take  $2^{(L/2)}$  attempts
  - **Efficient**
    - Computing  $H$  should be computationally efficient

# Message Authentication Codes vs. Signatures

- **Message Authentication Code (MAC)**

- Hash of message encrypted with a symmetric key:  
An intruder will not be able to replace the hash value

- **Digital Signature**

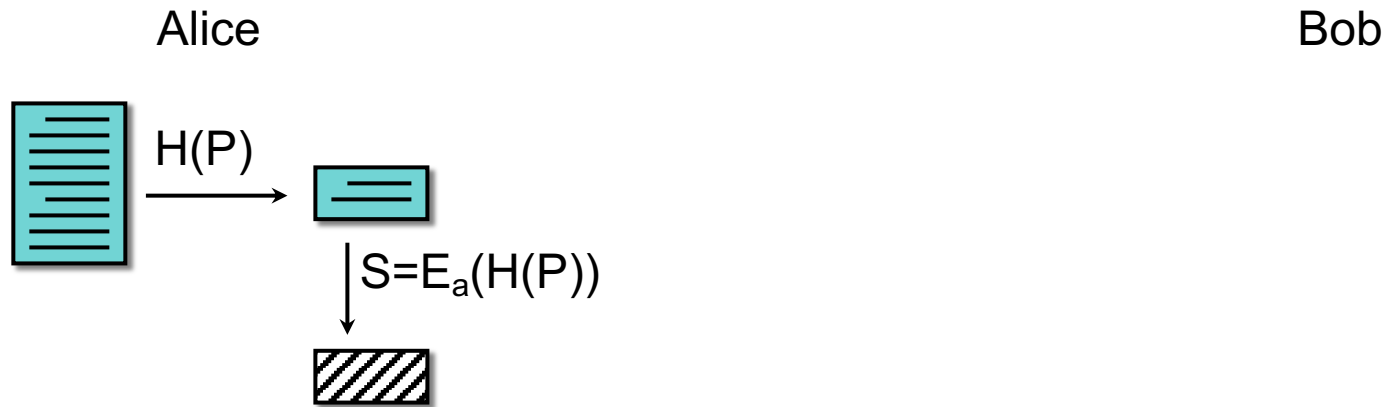
- Hash of message encrypted with the owner's private key
  - Alice encrypts the hash with her **private key**
  - Bob validates it by decrypting it with her public key & comparing with  $hash(M)$
- Provides **non-repudiation**: recipient cannot change the encrypted hash

# Digital signatures: public key cryptography



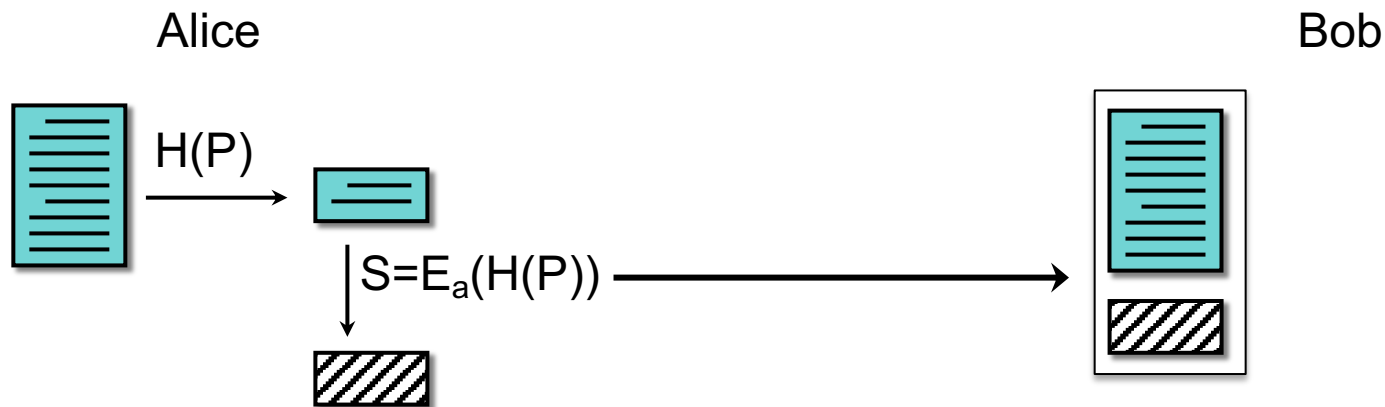
Alice generates a hash of the message

# Digital signatures: public key cryptography



Alice encrypts the hash with her private key  
This is her **signature**.

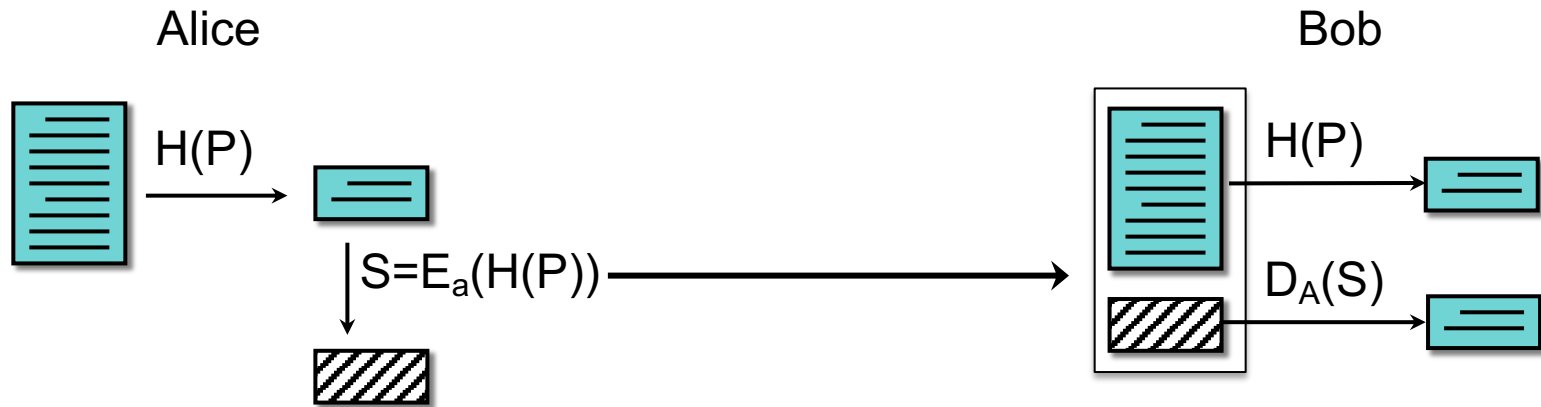
# Digital signatures: public key cryptography



Alice sends Bob the message & the encrypted hash

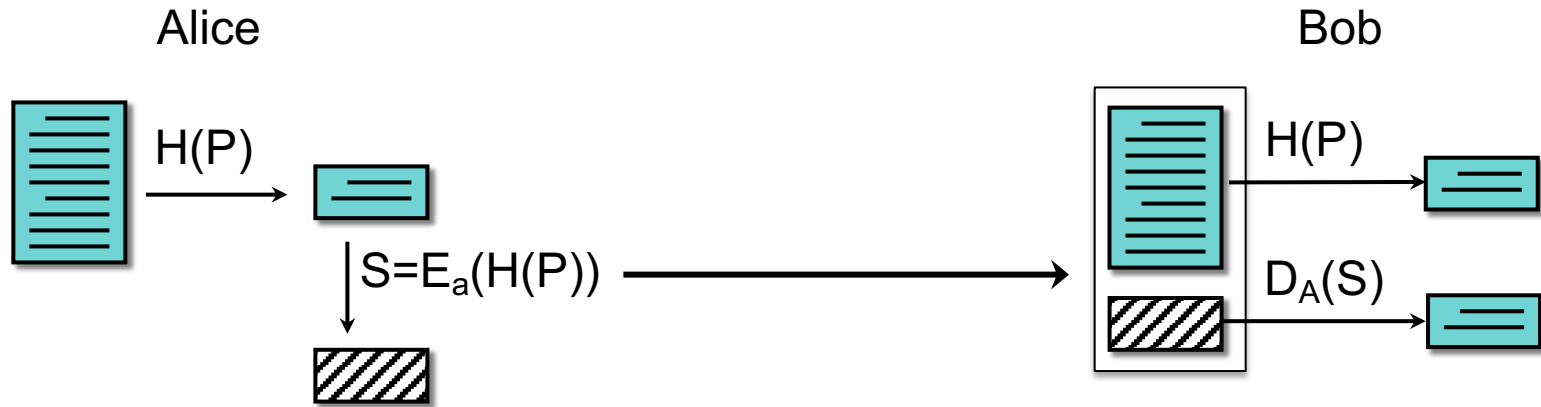


# Digital signatures: public key cryptography



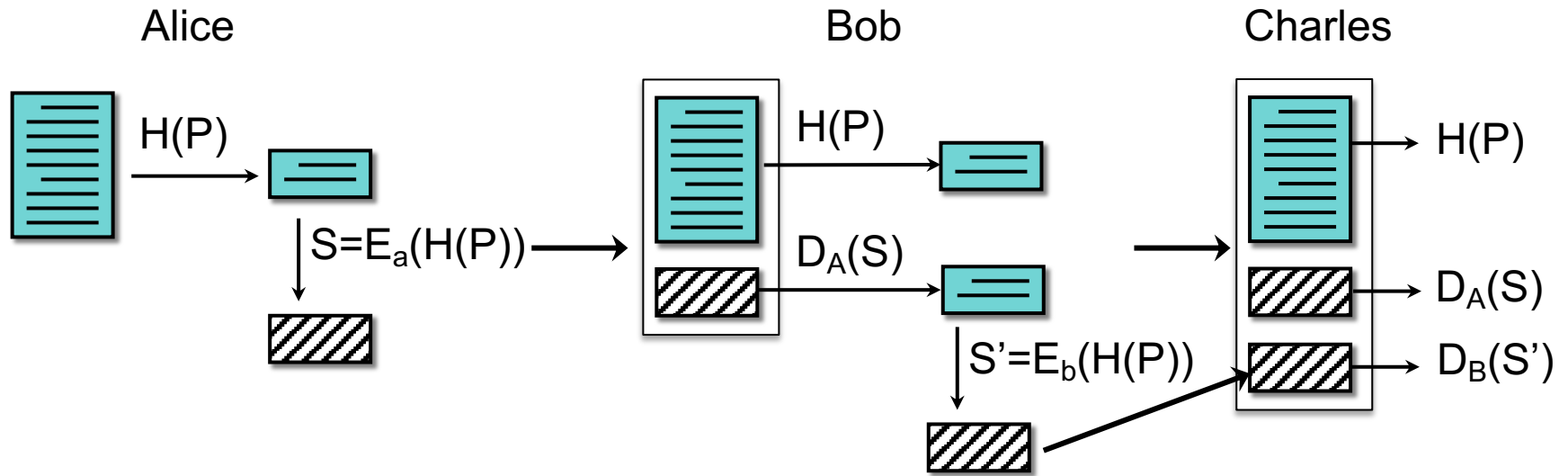
1. Bob decrypts the hash using Alice's public key
2. Bob computes the hash of the message sent by Alice

# Digital signatures: public key cryptography



If the hashes match, the signature is valid  
– the encrypted hash *must* have been generated by Alice

# Digital signatures: multiple signers



Charles:

- Generates a hash of the message,  $H(P)$
- Decrypts Alice's signature with Alice's public key
  - Validates the signature:  $D_A(S) \stackrel{?}{=} H(P)$
- Decrypts Bob's signature with Bob's public key
  - Validates the signature:  $D_B(S) \stackrel{?}{=} H(P)$

# Covert AND authenticated messaging

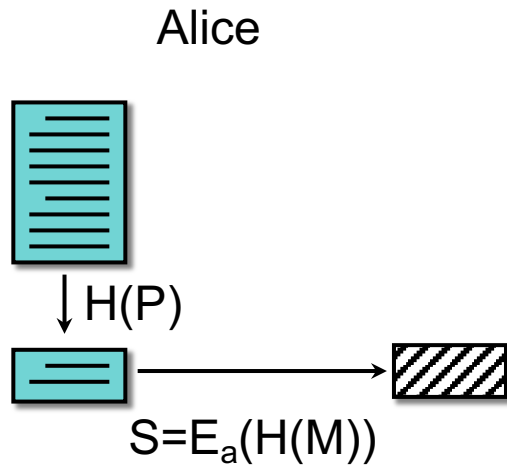
If we want to keep the message secret

- combine **encryption** with a **digital signature**

Use a session key:

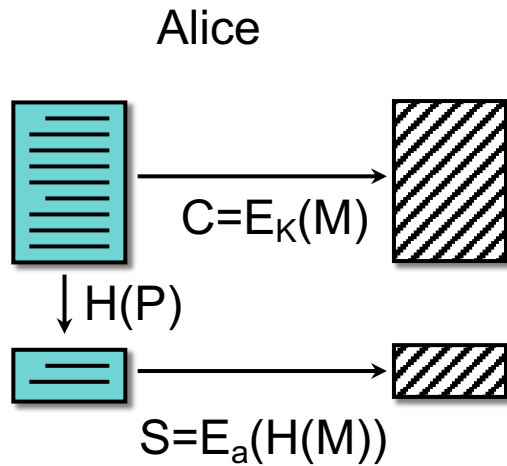
- Pick a **random key,  $K$** , to encrypt the message with a symmetric algorithm
- **encrypt  $K$**  with the public key of each recipient
- for signing, **encrypt the hash** of the message with sender's private key

# Covert and authenticated messaging



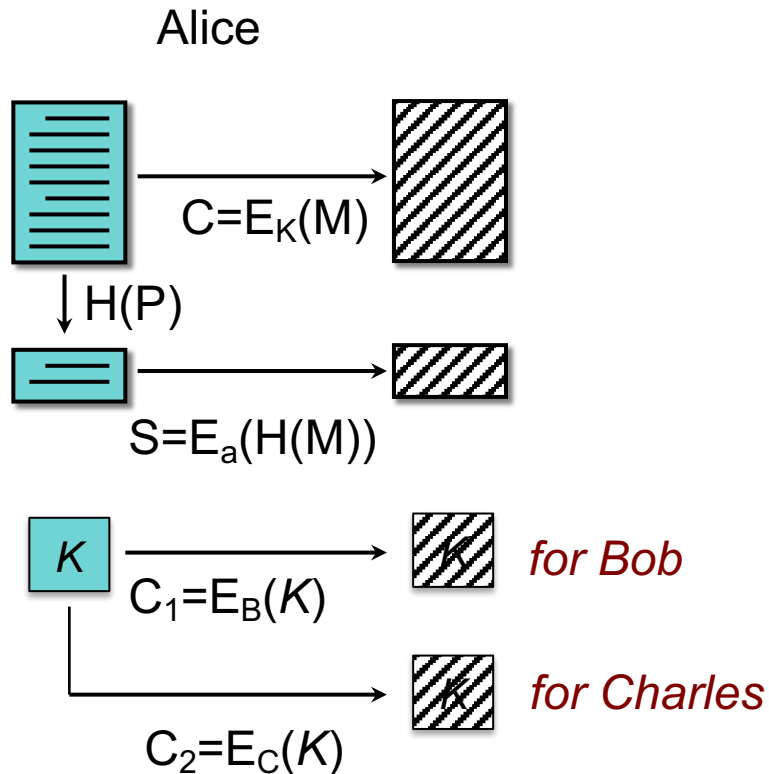
Alice generates a digital signature by encrypting the message with her private key

# Covert and authenticated messaging



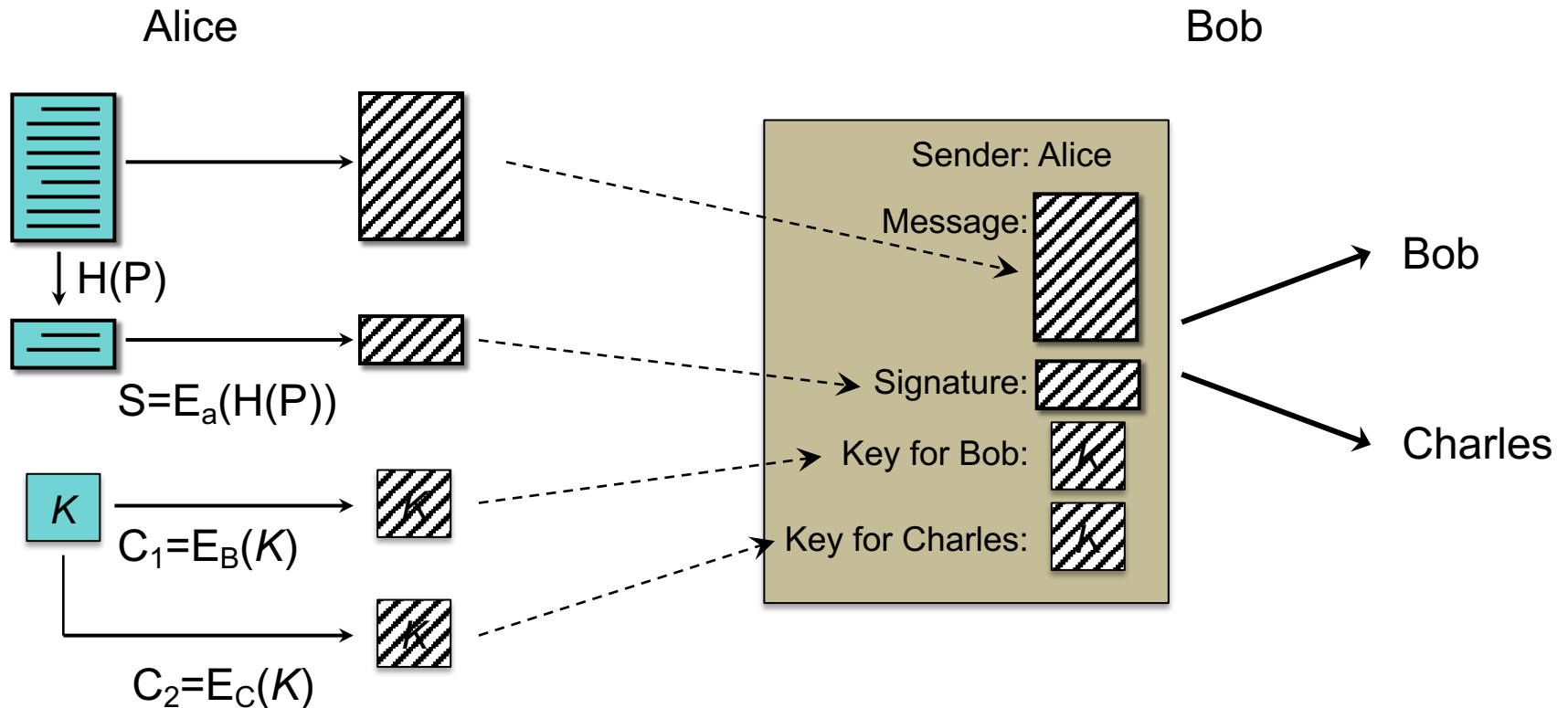
Alice picks a random key,  $K$ , and encrypts the message  $P$  with it using a symmetric cipher

# Covert and authenticated messaging



Alice encrypts the session key for each recipient of this message using their public keys

# Covert and authenticated messaging



The aggregate message is sent to Bob & Charles



The end